



Stellar Parameter Determination

Standard Methods &
NLTE Refinements

N. Przybilla & M.F. Nieva

Requirements for accurate analyses

- local temperature & particle densities need to be known
 - atmospheric structure
- radiation field realistic
 - $S_\nu \neq B_\nu(T)$

atmospheric
parameters

- all relevant processes taken into account for SE
 - high-quality atomic data available
 - ab-initio calculations
- any weakness affects overall accuracy



Why accurate analyses?

understand stars across HRD

- stellar atmospheres
- stellar structure
- stellar evolution
- nucleosynthesis
- cosmic cycle of matter
- galactic evolution
- cosmology
- ...



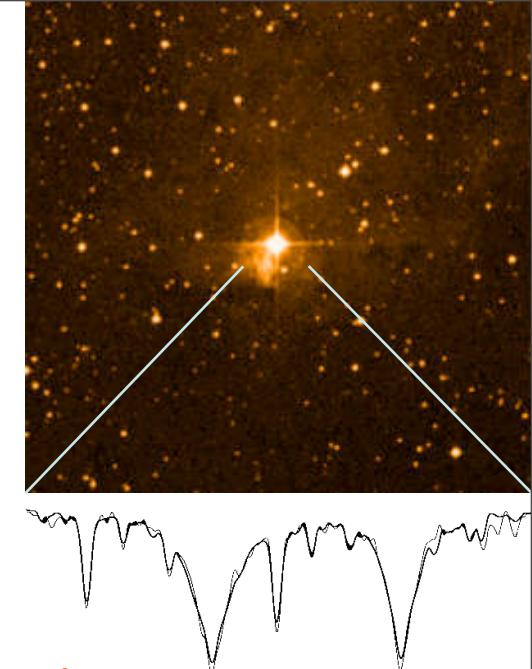
Diagnostic Problem

stellar analyses from
interpretation of observation

→ photometry, spectroscopy

- fundamental physical properties: M, L, R (Ω, B)
 → direct methods only for few stars
- atmospheric parameters: $T_{\text{eff}}, \log g, \xi, Y, Z, \dots$
- chemical composition

→ quantitative spectroscopy
via model atmospheres



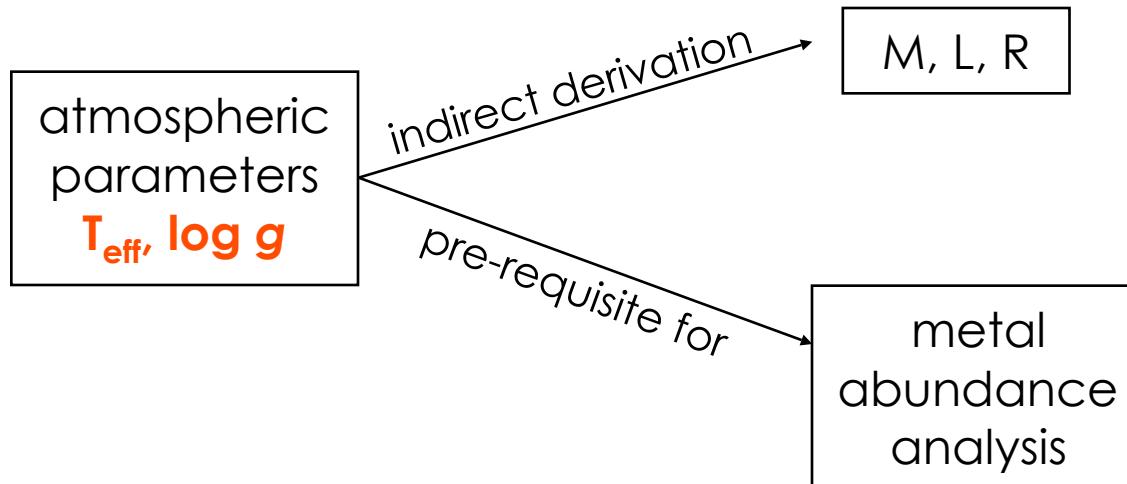
Fundamental determinations of stellar parameters

- from detached eclipsing binary systems ➔ M, R
- for standard stars:
 - Sun
 - Vega
 - Procyon
 - Arcturus
 - & a few other ...



Characterisation of a Star

Praxis

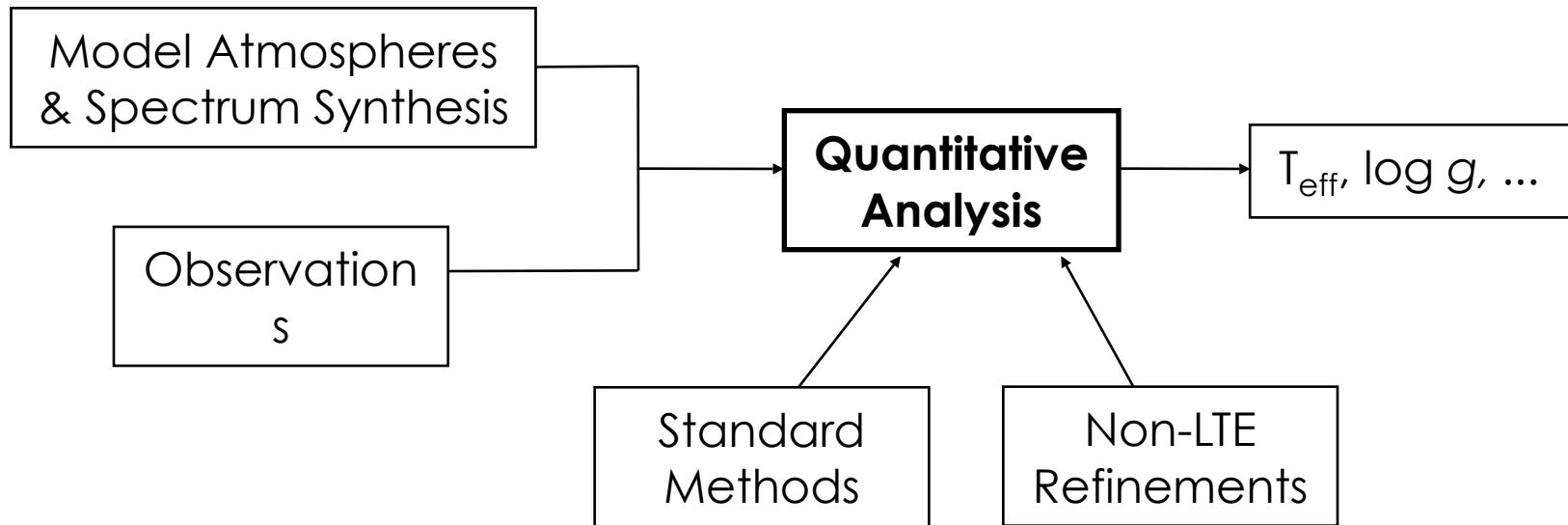


T_{eff} & log g: - define physical conditions of stellar atmosphere

also: microturbulence, global metallicity, H & He abundance

→ T & P-stratification

Atmospheric Parameter Determination



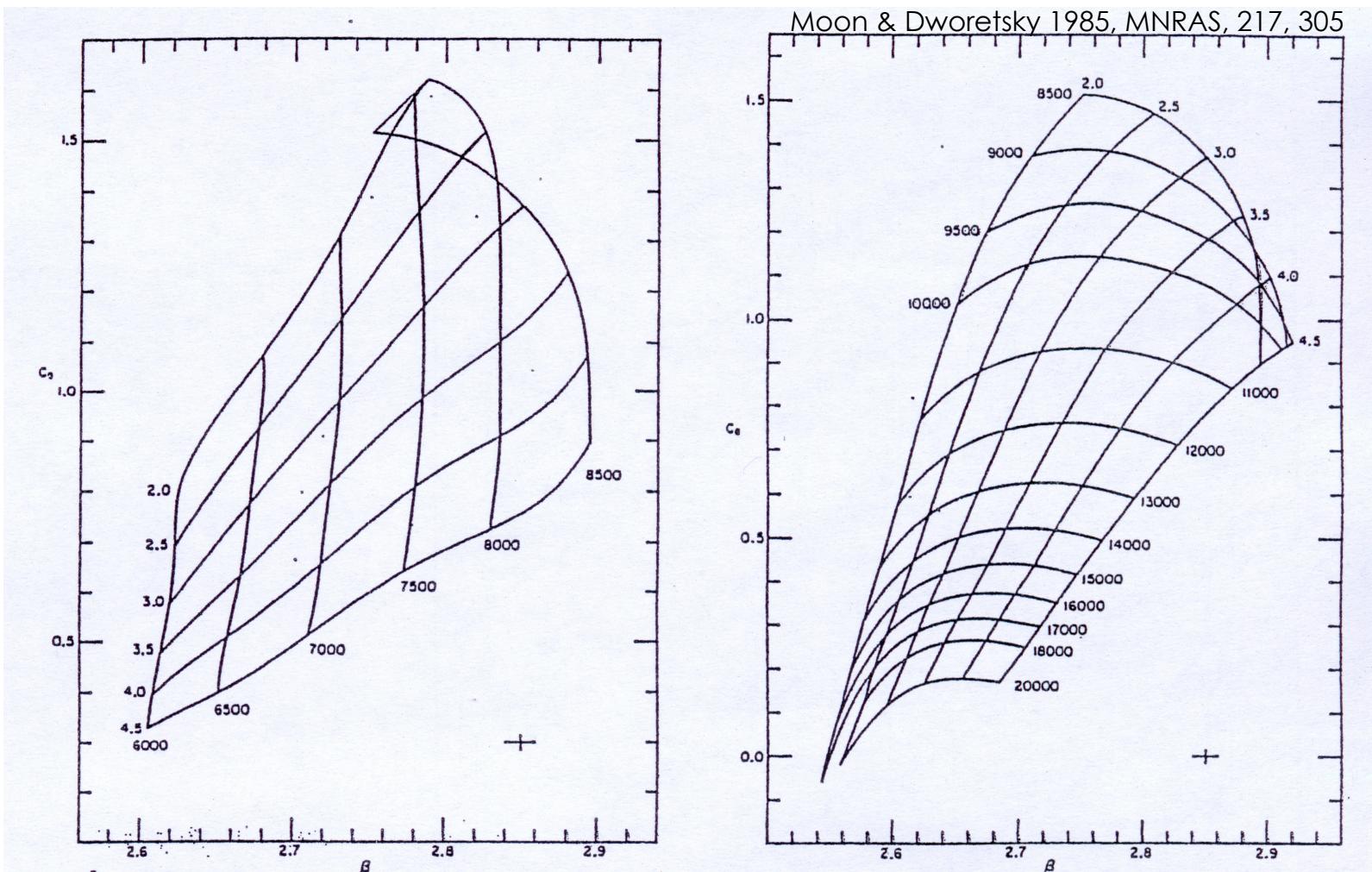
Photometric Techniques

Photometry

- idea: sample stellar flux distribution by a few bandpasses
- observationally ‘cheap’: easy to obtain for large numbers of objects
- availability of large amounts of data:
 - broadband: e.g. Johnson
 - smallband: e.g. Strömgren
 - IR: e.g. 2MASS
- calibrated on basis of line-blanketed LTE model atmospheres
- highly useful for analysis of large stellar samples
- accuracy: ~1... x%



Smallband photometry: e.g. Strömgren



- comparison of different calibrations by Napiwotzki et al. 1993, A&A, 268, 653

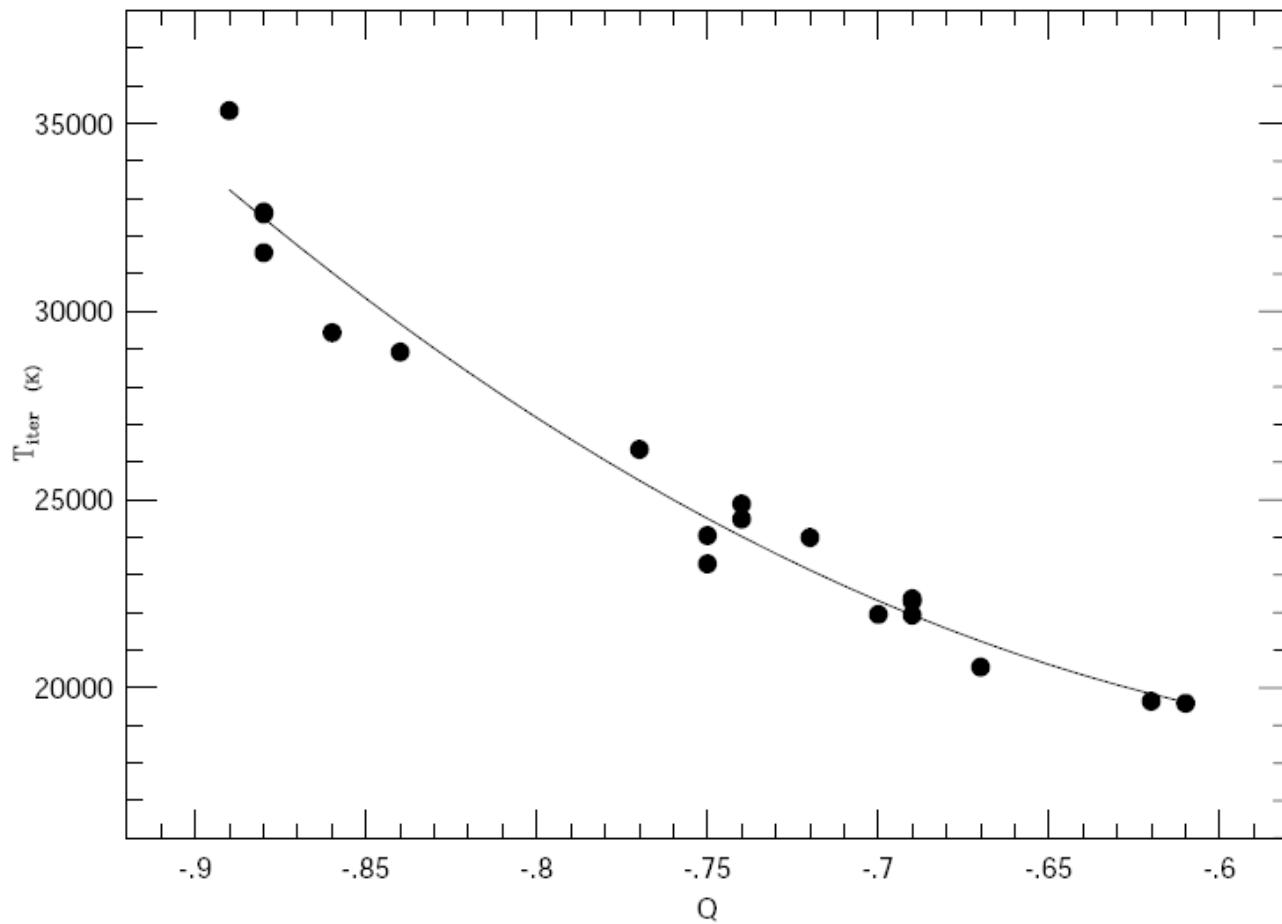
➤ uncomfortable disagreement

➤ improvements



Broadband photometry: e.g. Johnson

Daflon et al. 1999, ApJ, 522, 950



$$Q = (U-B) - 0.72(B-V) \quad - \text{reddening free}$$

Comparison of different T_{eff} -indicators in B stars

Poster by M.I. Zavallos Herencia & S. Daflon

	T_Q	T_L	T_S	T_{S-N}	$T_{\text{Si-LTE}}$	$T_{\text{Si-NLTE}}$	$\epsilon(\text{O II})_{\text{LTE}}$
NGC2244-376	30010	27650	33900	29410	32950	-	8.33 ... 8.83
NGC2244-201	29670	27380	27260	27170	27800	28300	8.76 ... 8.81



$\Delta T > 5000\text{K}$ possible

line-to-line scatter: $1\sigma(\text{abundance})$: $\sim 0.1 \dots \sim 0.5\text{dex}$

Spectrophotometry

- ground-based spectrophotometry highly useful

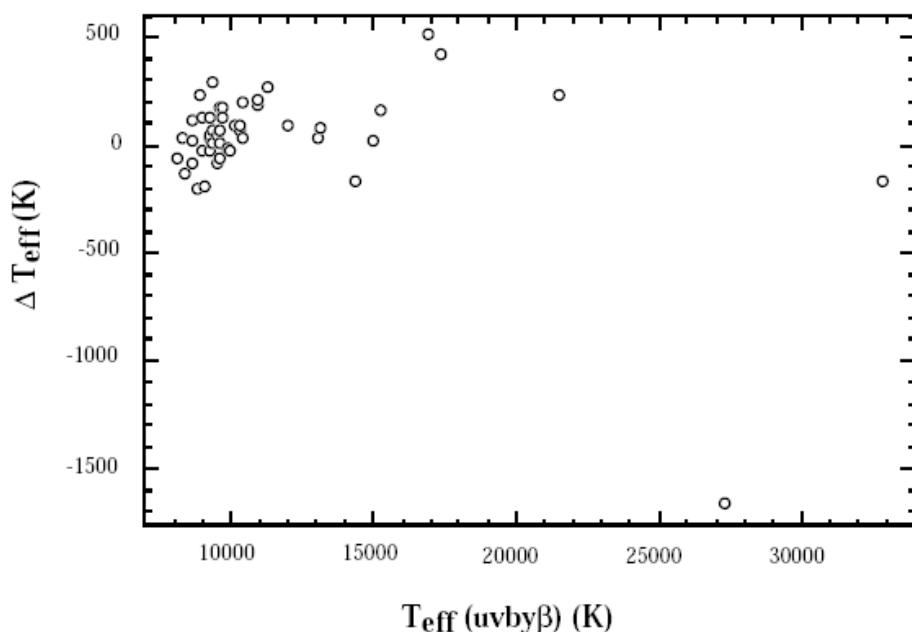


Fig. 5. The differences (ΔT_{eff} (K)) (photometric minus spectrophotometric-Hy values) of the effective temperatures as a function of the photometric temperature T_{eff} ($\text{uvby}\beta$) (K).

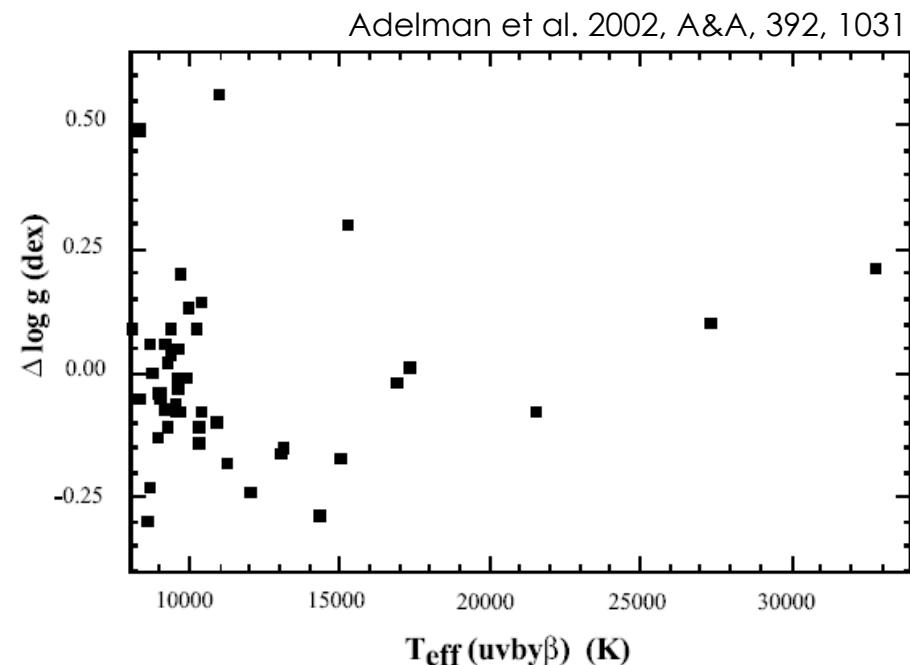


Fig. 6. The differences ($\Delta \log g$ (dex)) (photometric minus spectrophotometric-Hy values) of the surface gravities as a function of the photometric temperature T_{eff} ($\text{uvby}\beta$) (K).

- flux-calibrated data in UV : IUE, HST, FUSE, ...

→ hot stars

Other methods:

- IRFM
- T_{eff} - colour relations
- spectral type – T_{eff} relations
- line ratios
- excitation temperatures



Spectroscopic Techniques

Kurucz 1979, ApJS, 40, 1

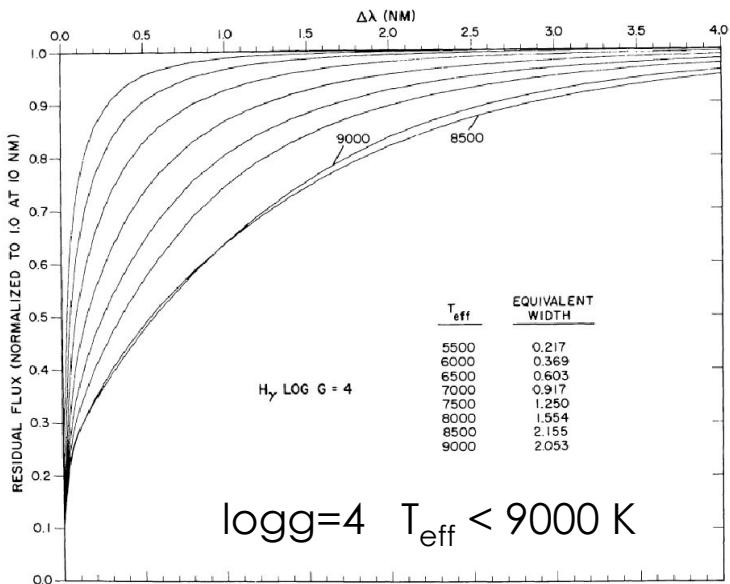


FIG. 21.— $H\gamma$ profiles for solar abundance models with $T_{\text{eff}} \leq 9000$ K. Equivalent widths are given in nm.

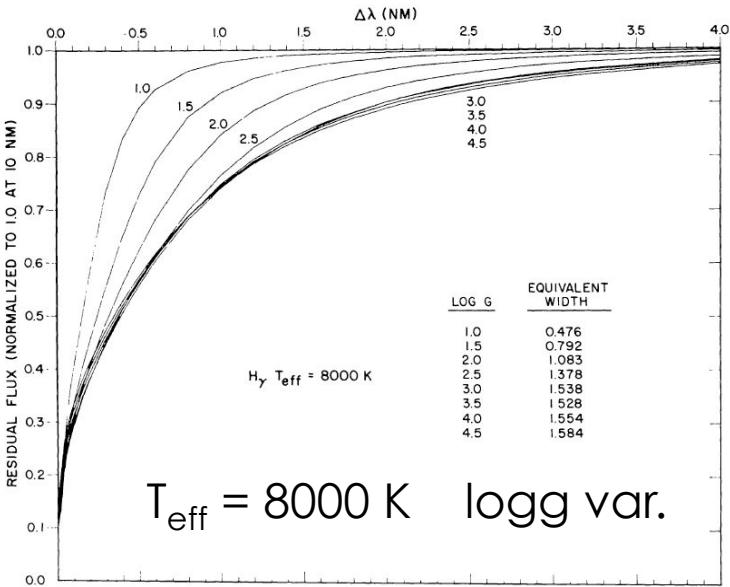


FIG. 24.— $H\gamma$ profiles as a function of gravity for $T_{\text{eff}} = 8000$ K

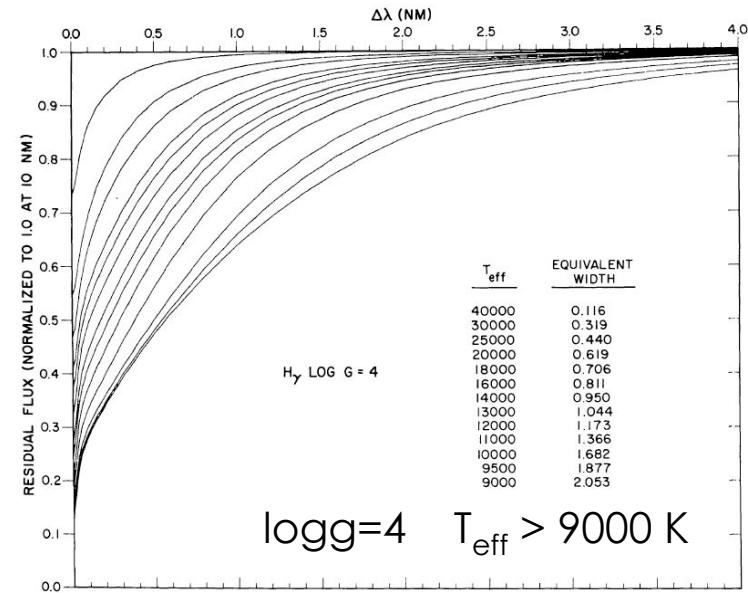
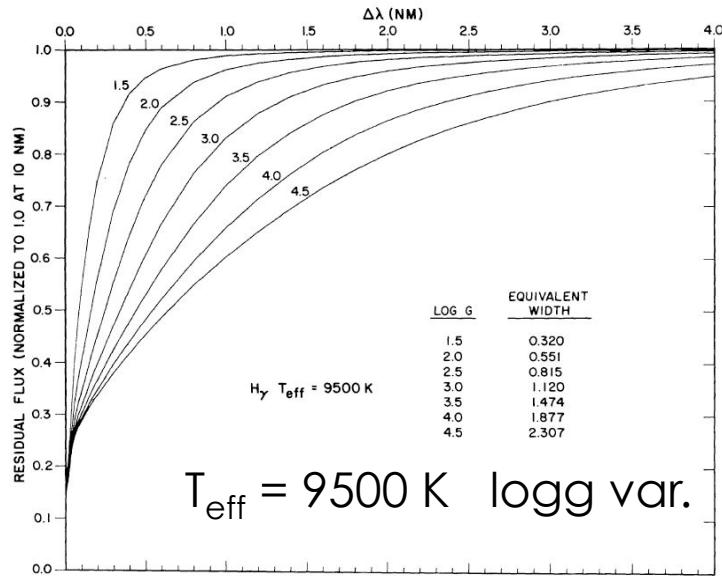


FIG. 23.— $H\gamma$ profiles for the early-type models showing the decrease in equivalent width with increasing T_{eff}



— $H\gamma$ profiles as a function of gravity for $T_{\text{eff}} = 9500$ K, roughly A0, where the profile is ideal for gravity determination



T_{eff} determination: Balmer lines vs. photometric calibrations

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Sun

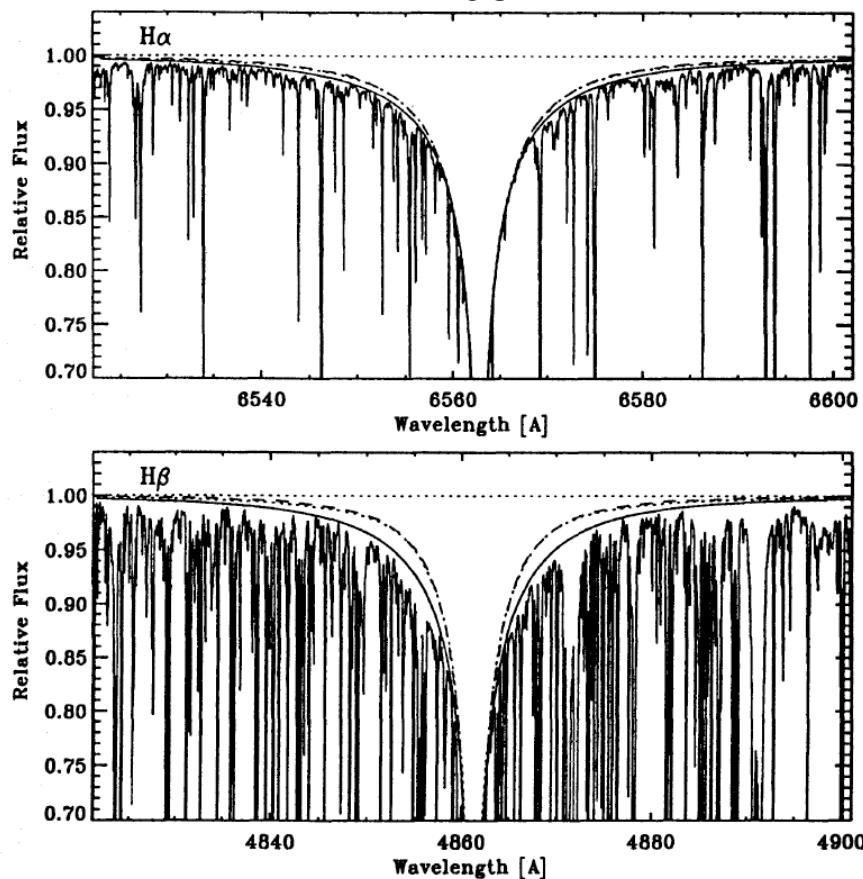


Fig. 2. Solar $H\alpha$ (top) and $H\beta$ (bottom) line profiles compared with synthetic fit profiles from 3 different solar model atmospheres, Holweger & Müller (1974, dots), Kurucz (1979, $\alpha = 2$, dashes), and our own ODF model ($\alpha = 0.5$, continuous line)

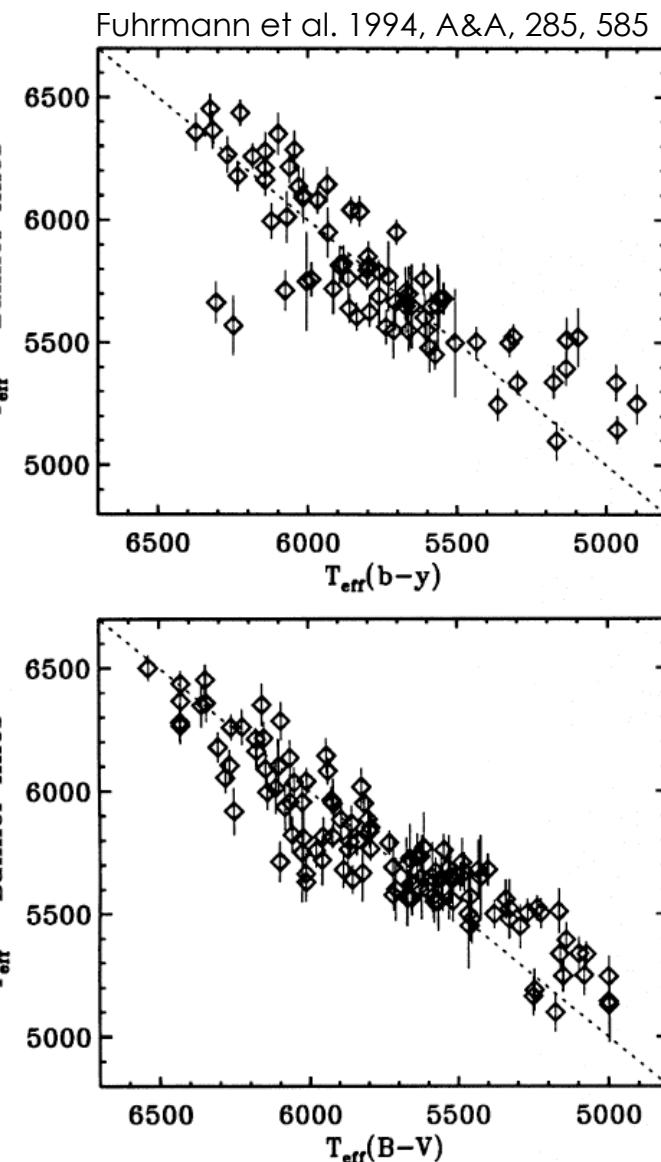
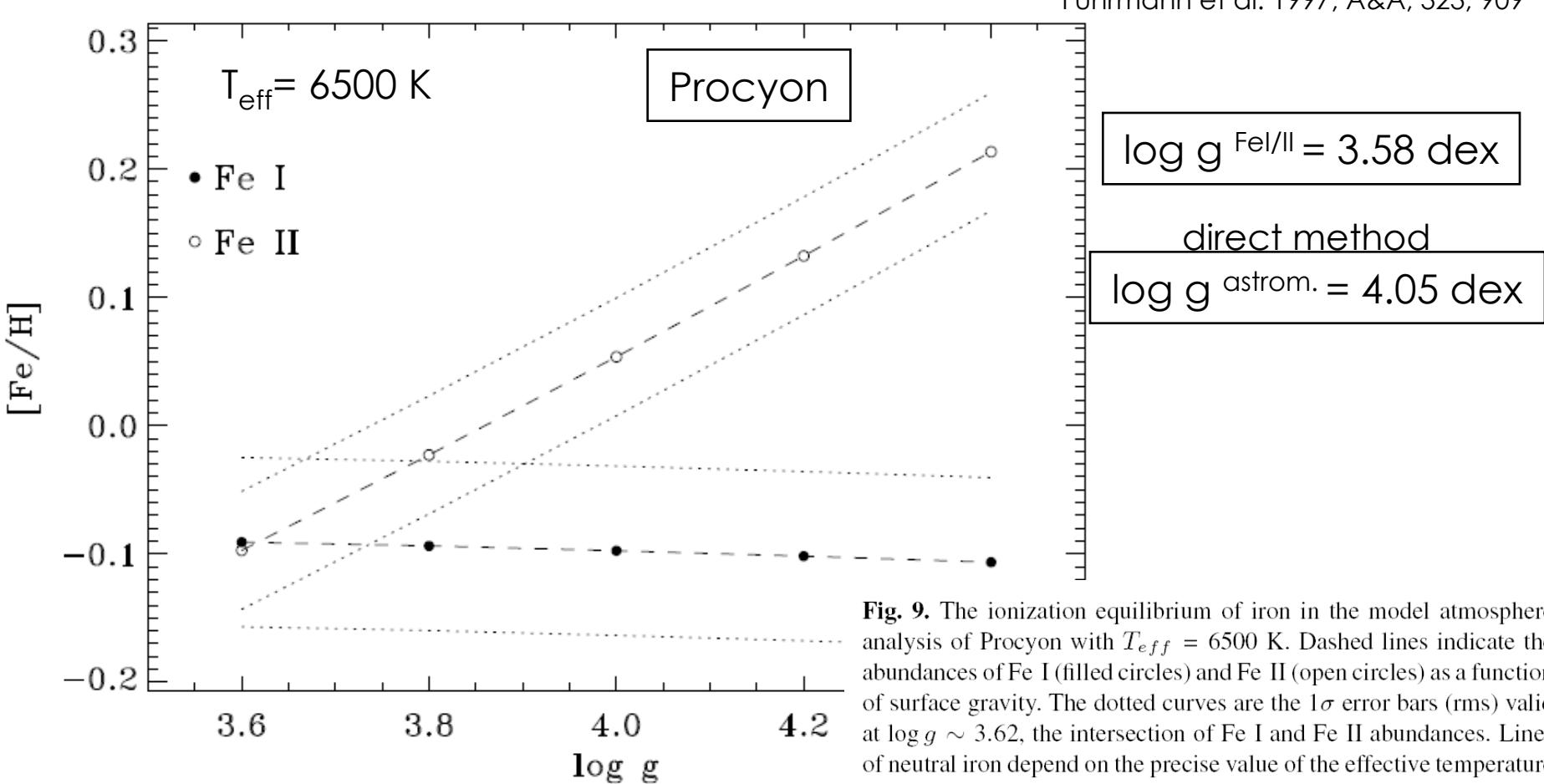


Fig. 4. Effective temperatures obtained from Balmer line fits are compared with colour temperatures derived from $b - y$ (top) and $B - V$ (bottom). The calibration of Magain (1987) is used here (see text)

$\log g$ determination: LTE Fe I/II ionization equilibrium

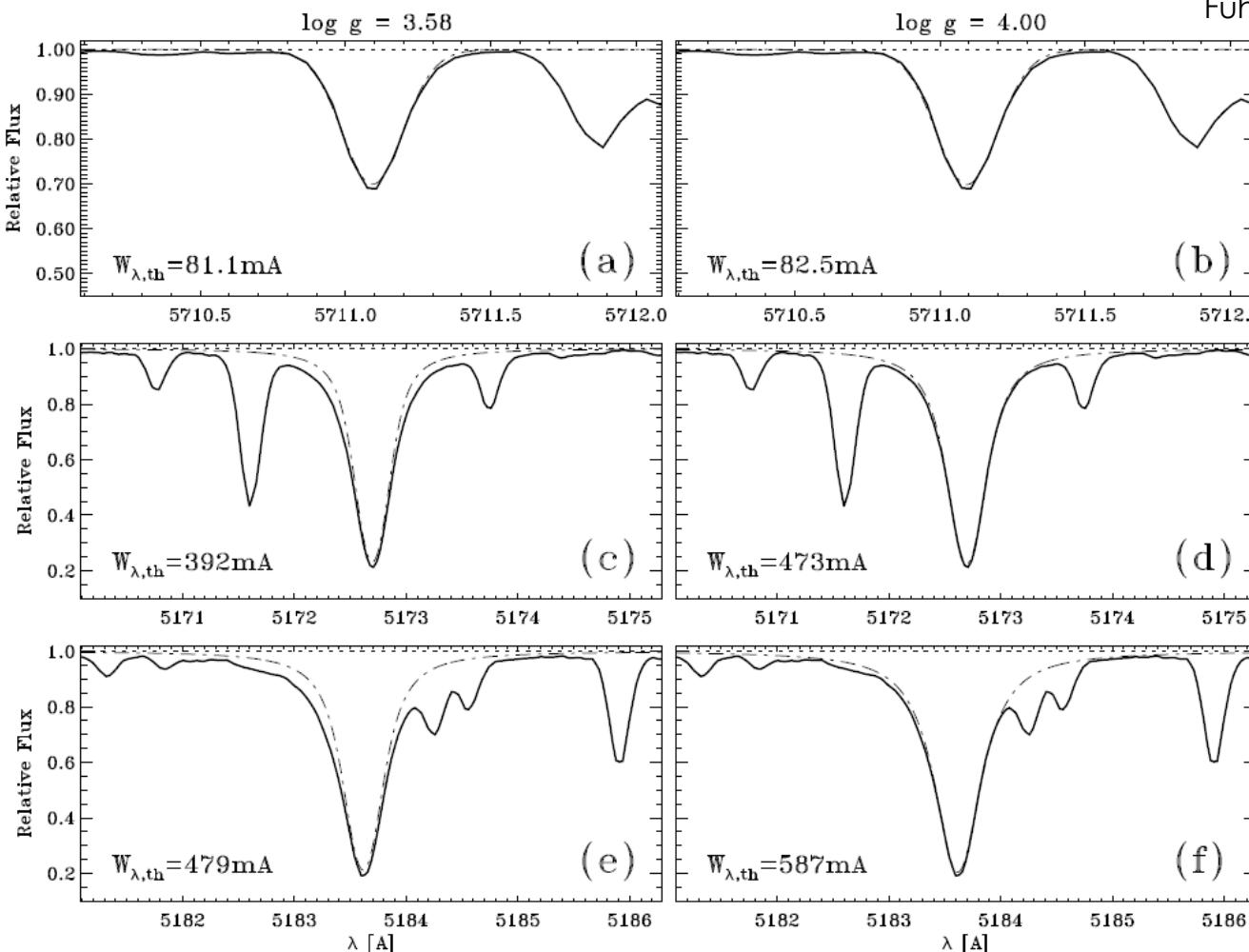


ionization equilibrium:
same abundance from all ions
at **one** set of parameters

Fig. 9. The ionization equilibrium of iron in the model atmosphere analysis of Procyon with $T_{\text{eff}} = 6500 \text{ K}$. Dashed lines indicate the abundances of Fe I (filled circles) and Fe II (open circles) as a function of surface gravity. The dotted curves are the 1σ error bars (rms) valid at $\log g \sim 3.62$, the intersection of Fe I and Fe II abundances. Lines of neutral iron depend on the precise value of the effective temperature with $\Delta[\text{Fe}/\text{H}] \sim 0.06 \text{ dex}$ for a change of $\Delta T_{\text{eff}} = 100 \text{ K}$. Fe II instead is very sensitive to the surface gravity parameter, but almost independent to a change in the effective temperature ($\Delta[\text{Fe}/\text{H}] < 0.01 \text{ dex}$ for $\Delta T_{\text{eff}} = 200 \text{ K}$). The discrepancy at $\log g = 4.05$, the astrometric surface gravity of Procyon, amounts $\Delta[\text{Fe}/\text{H}] = 0.17 \text{ dex}$. To reconcile the Fe I and Fe II abundances an unrealistic high effective temperature of $\sim 6800 \text{ K}$ would be required



log g determination: Mg line wings



Fuhrmann et al. 1997, A&A, 323, 909

$T_{\text{eff}} = 6500 \text{ K}$

$\log g^{\text{Mg}} = 4.00 \text{ dex}$

direct method

$\log g^{\text{astrom.}} = 4.05 \text{ dex}$

consistency in LTE

Fig. 10a–f. The spectroscopic surface gravity determination of Procyon from the analysis of Mg I lines. Left column: line profiles of Mg I $\lambda 5711$ (top) and the Mg Ib lines $\lambda 5172$ and $\lambda 5183$ (below) for a surface gravity value $\log g = 3.58$, as derived from the ionization equilibrium. The profile of $\lambda 5711$ shows no wings and is practically independent of the surface gravity, as illustrated in panel b, where line formation is done for a value $\log g = 4.00$. Among other weak Mg I lines, $\lambda 5711$ therefore serves to fix the value of the Mg I abundance. This information is then used in the analysis of $\lambda 5172$ and $\lambda 5183$ by altering the surface gravity value until the observed line shape is reproduced as shown in panels d and f. In the case of Procyon $\log g = 4.00$ is found by this method, which is 0.42 dex higher than derived from the ionization equilibrium and only slightly below $\log g = 4.05$, the very precisely known value from astrometric data
Dr. Remeis-Sternwarte Bamberg



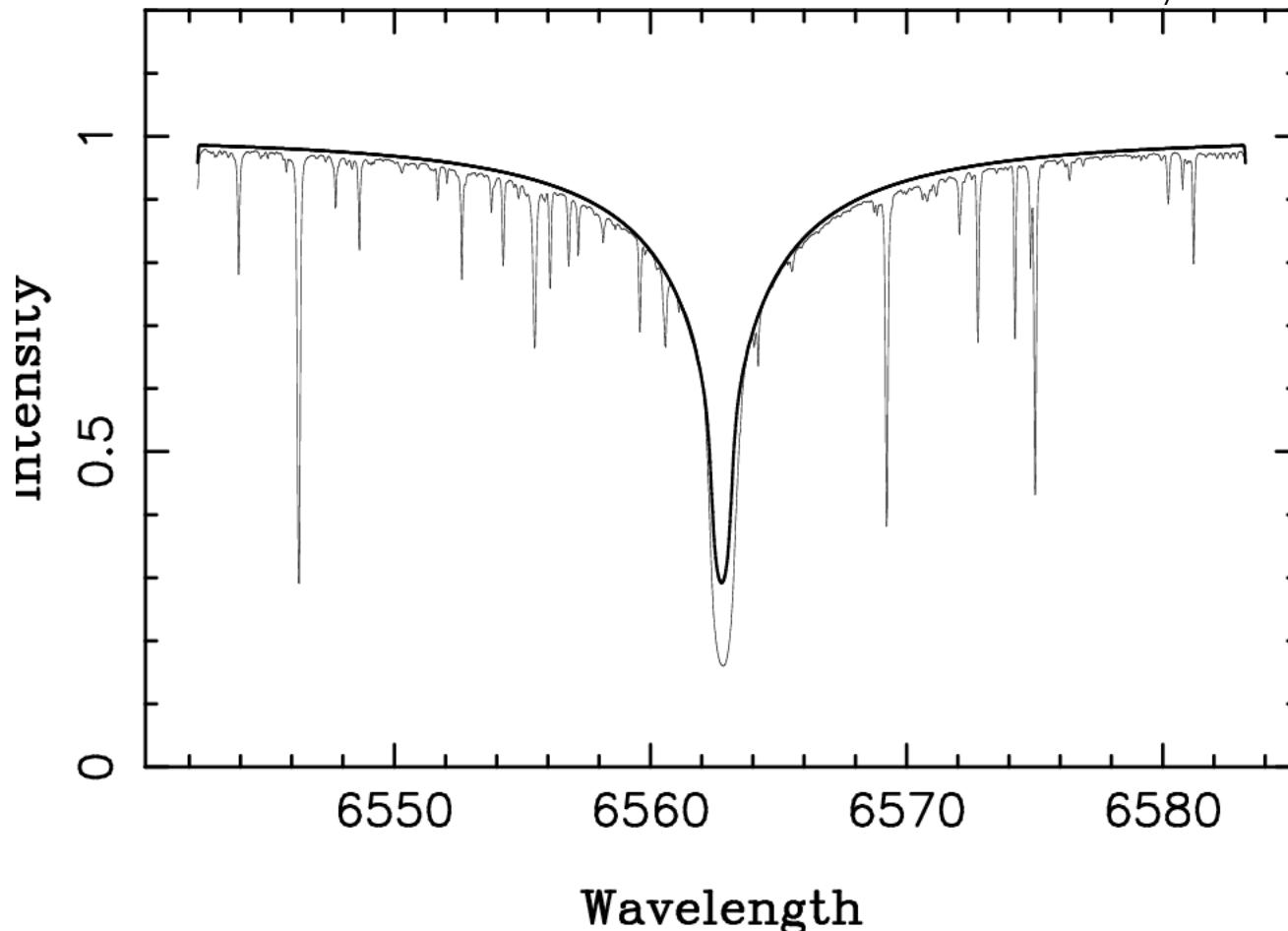
NLTE Refinements



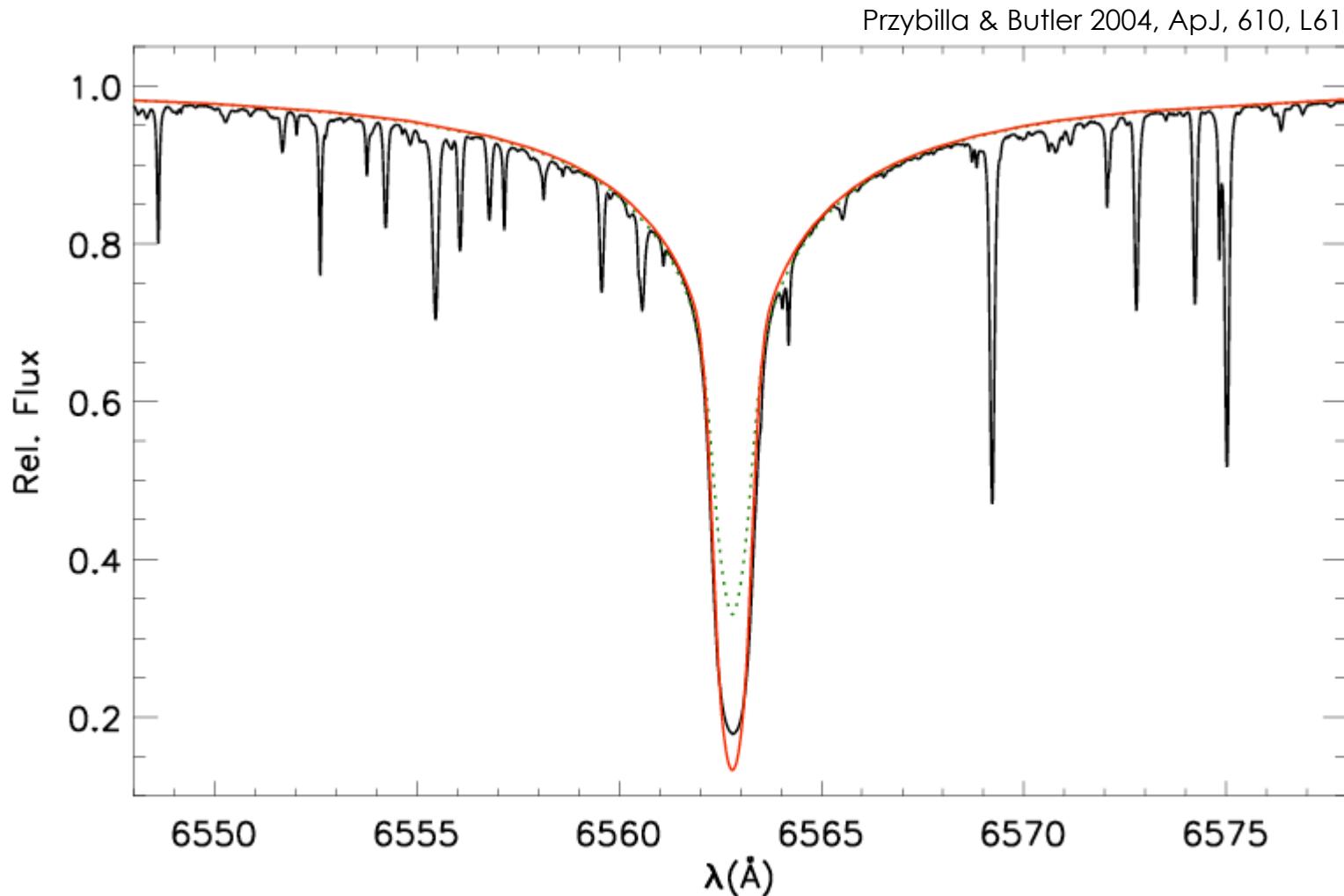
Status of H α modelling in the Sun: LTE ...

Stehle (Stark) + BPO (neutrals)

Cowley & Castelli 2002, A&A, 387, 595



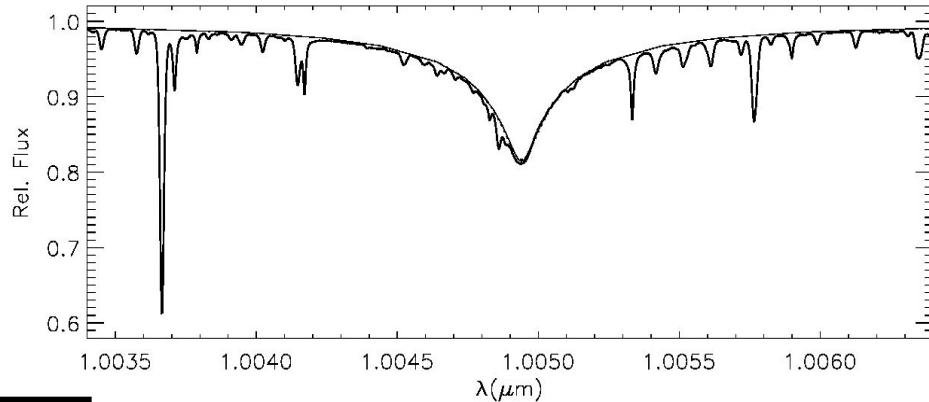
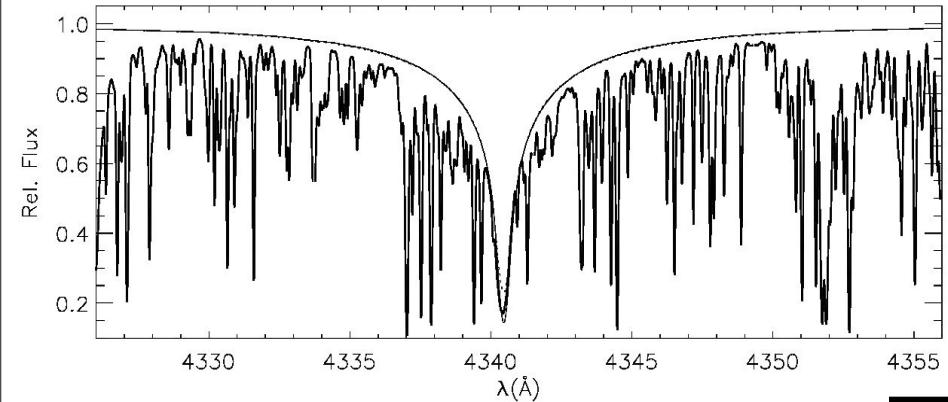
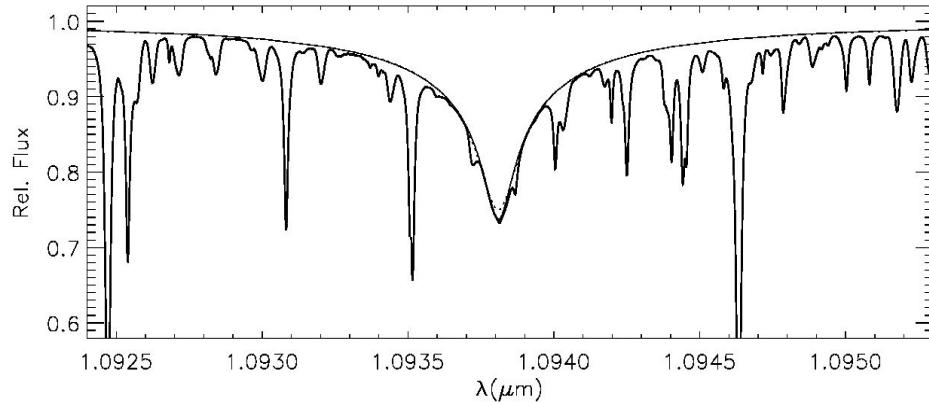
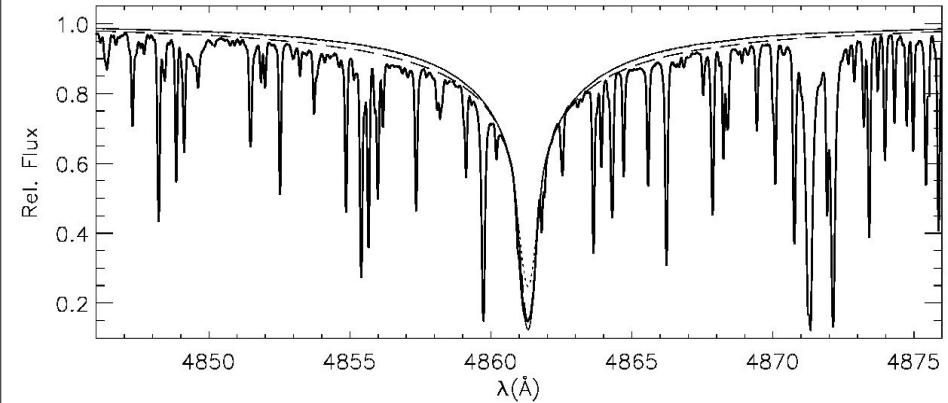
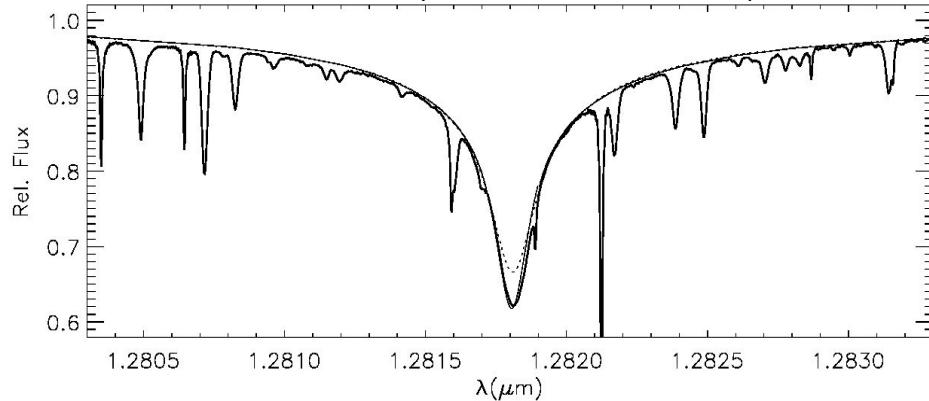
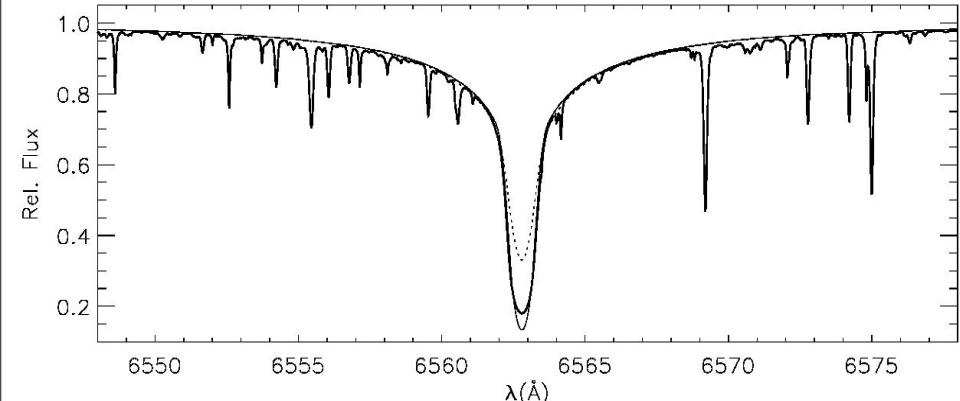
... and NLTE



- chromosphere important:
line-formation depth as observational discriminator

Sun: the broader picture in NLTE

Przybylla & Butler 2004, ApJ, 610, L61



$S_H=2$

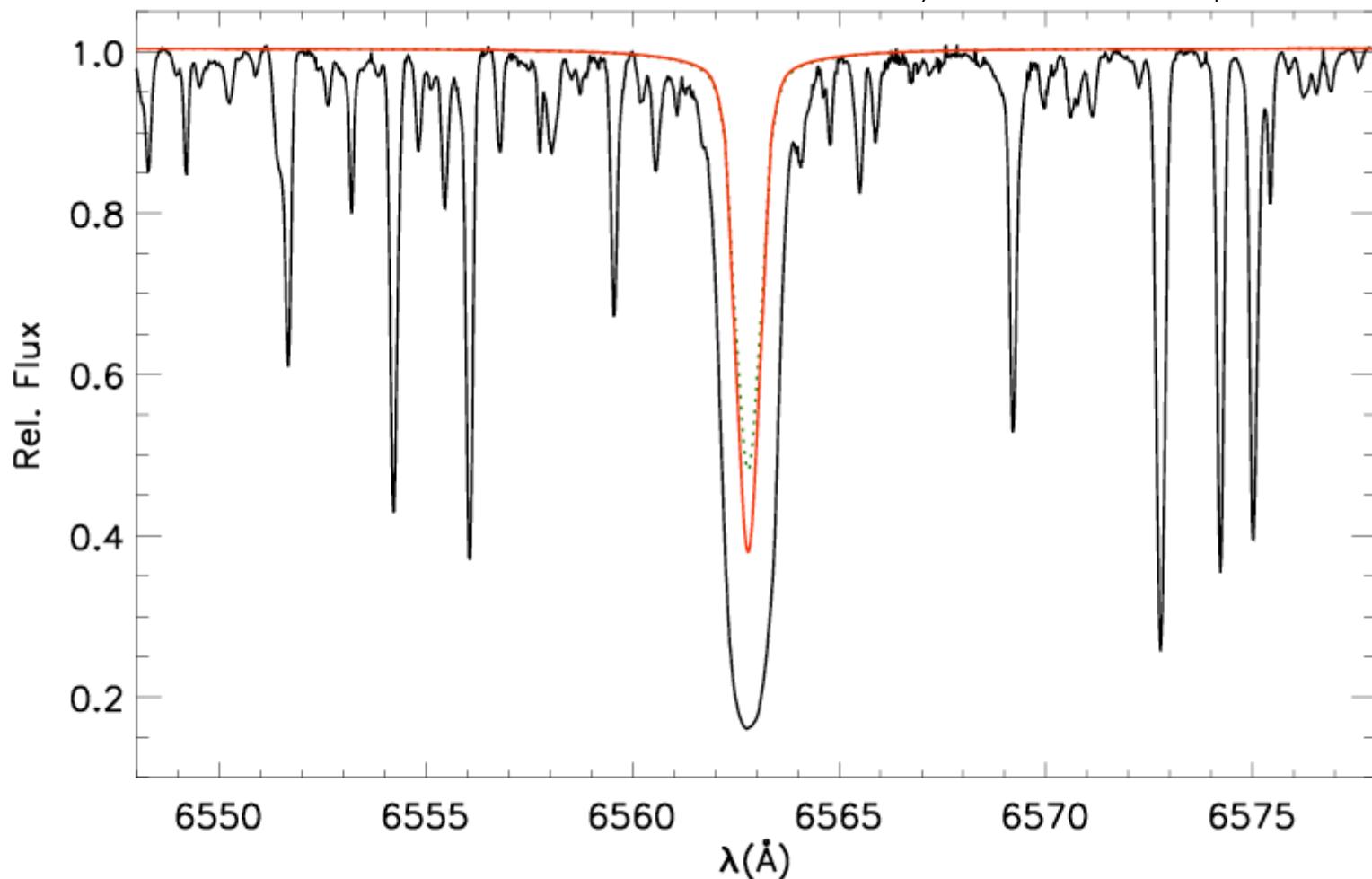


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N. Przybylla & M.F. Nieva - NLTE workshop – Nice 2007

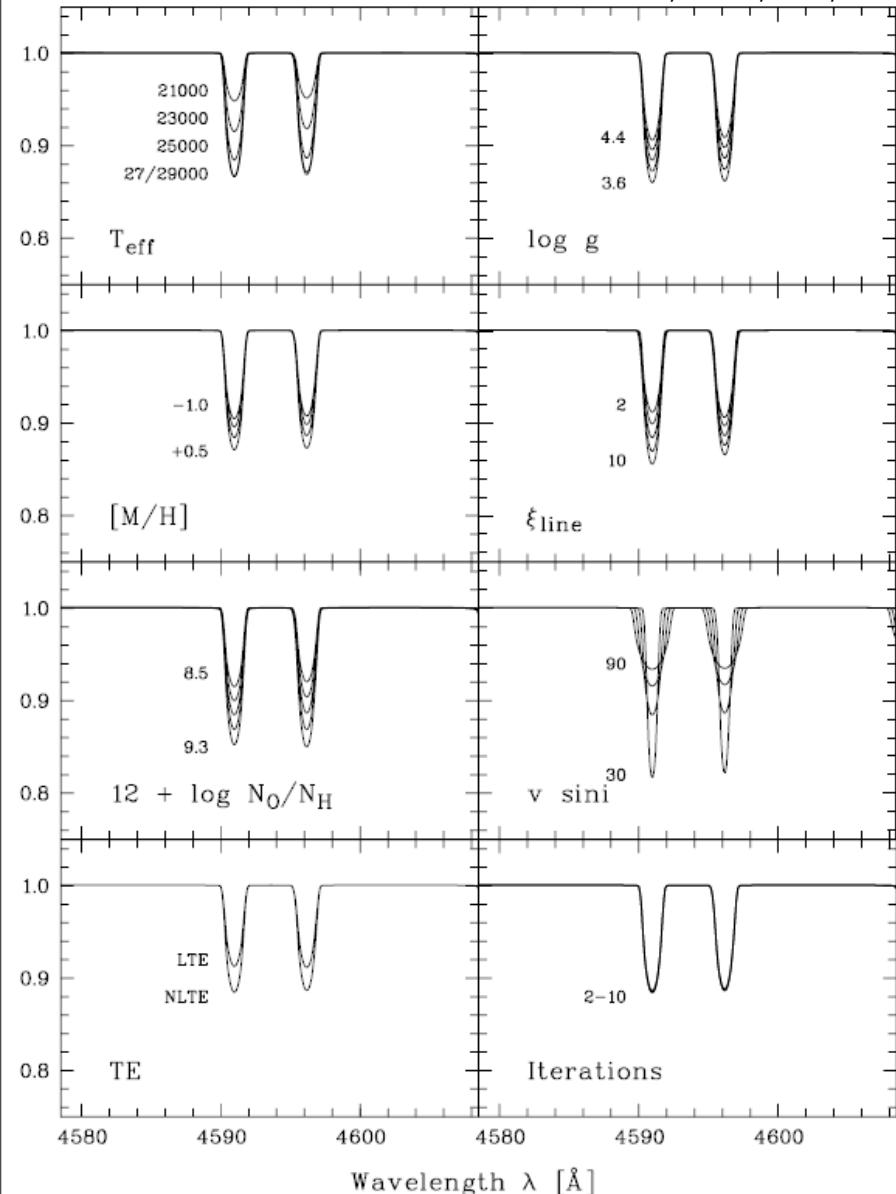
Arcturus: metal-poor K giant

Przybilla & Butler 2004, ApJ, 610, L61



- model atmosphere (Kurucz) used reproduces metal line spectrum





Effects to consider for stellar parameter/abundance determination

NLTE one among many factors

→ all need to be met

$T_{\text{eff}} = 25000$ K, $\log g = 4.0$

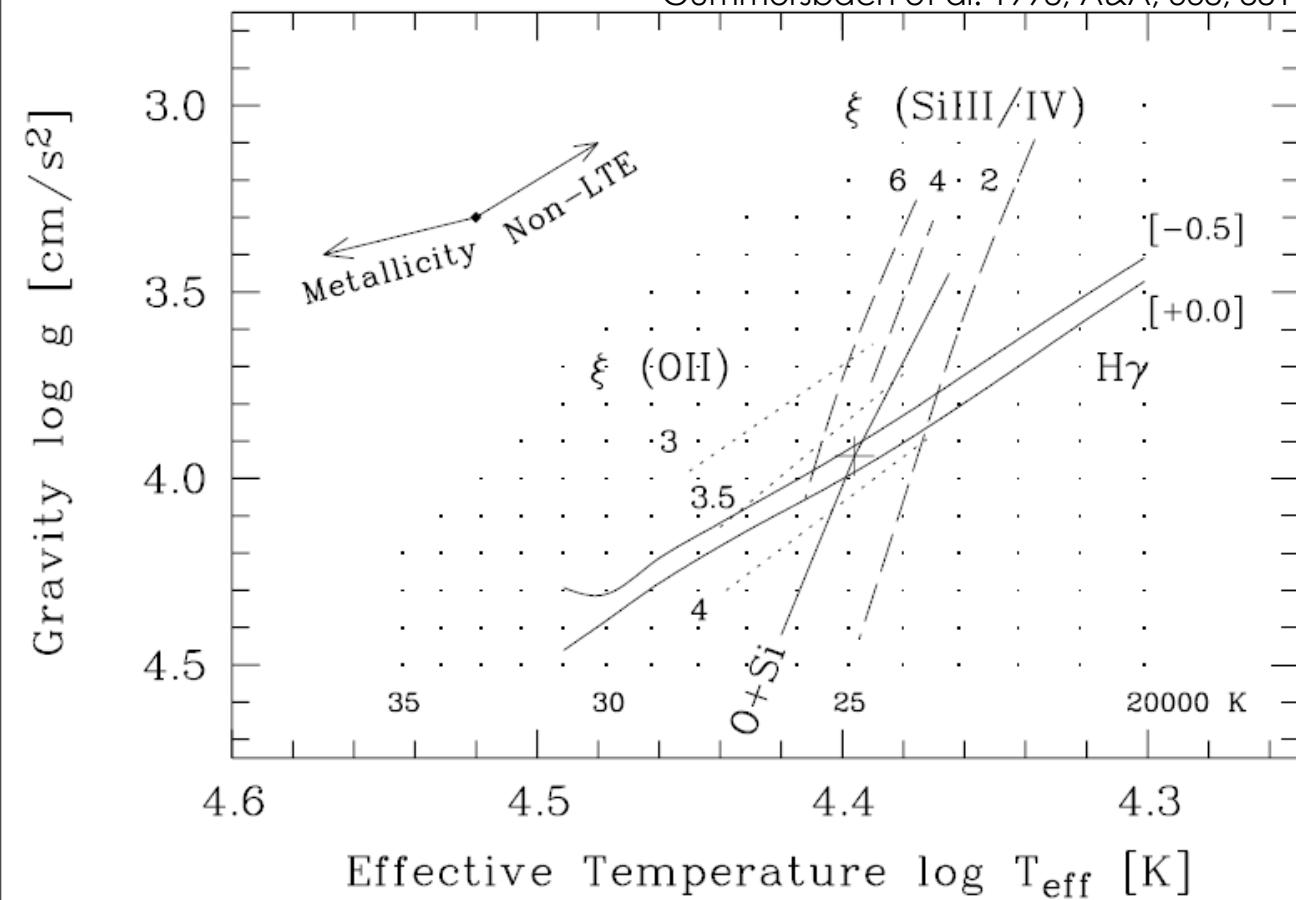
using Becker & Butler model atoms

Fig. 4. Same as Fig. 3, for O II 4591/96 and $X_O = 8.9$. Note the different behavior of $[M/H]$.



Kiel diagram

highly useful for
diagnostics



$T_{\text{eff}} = 25000 \text{ K}$, $\log g = 4.0$

using Becker & Butler
model atoms

Fig. 8. Overall analysis: Hydrogen analysis as function of $[M/H]=0$ and -0.5 (*solid*), silicon analysis as function of ξ (*dashed*), oxygen analysis as function of ξ (*dotted*), combined silicon and oxygen analysis (*solid*), and the derived stellar parameters (+) for SH 2-208/6. The arrows denote the metallicity effect of sub-solar atmospheres and the non-LTE effect discussed in Sect. 9.

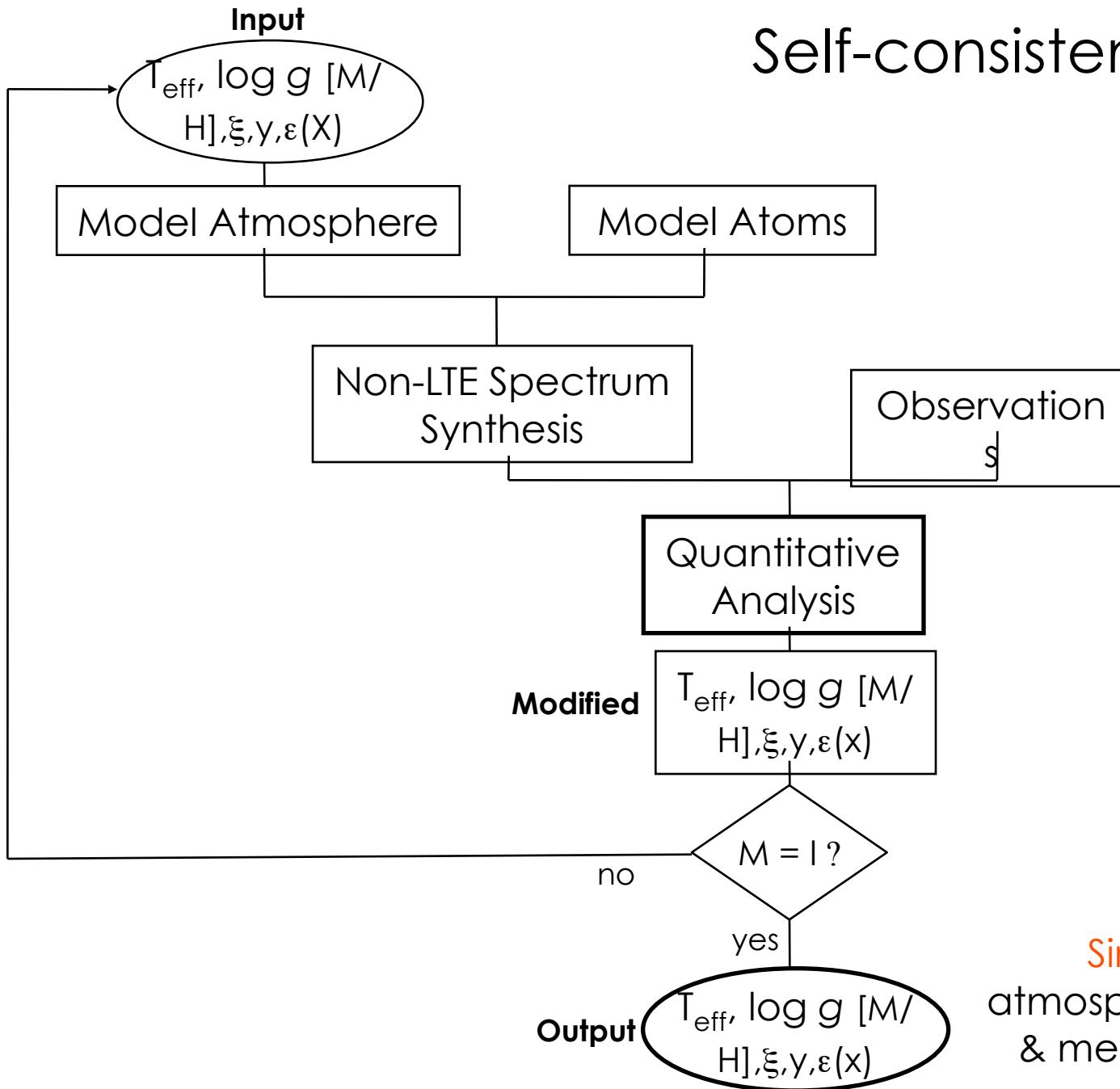
Explicitly... chemical abundances rely on:

- model atmospheres
- model atoms
- solution SE & RT: numerics
- other input: e.g. background opacities
- quantitative analysis (e.g. atmospheric parameters adopted)
- quality of observed spectra
- ...

All are potential sources of
systematic uncertainties



Self-consistent method



Simultaneous
atmospheric parameter
& metal abundance
derivation



Quantitative analysis

Independent constraints for atmospheric parameters:

- H & He lines
- multiple ionization equilibria
- SEDs

$$\bullet \Delta T_{\text{eff}} / T_{\text{eff}} \sim 1\%$$

$$\bullet \Delta \log g \sim 0.05...0.10 \text{ (cgs)}$$

} can be achieved



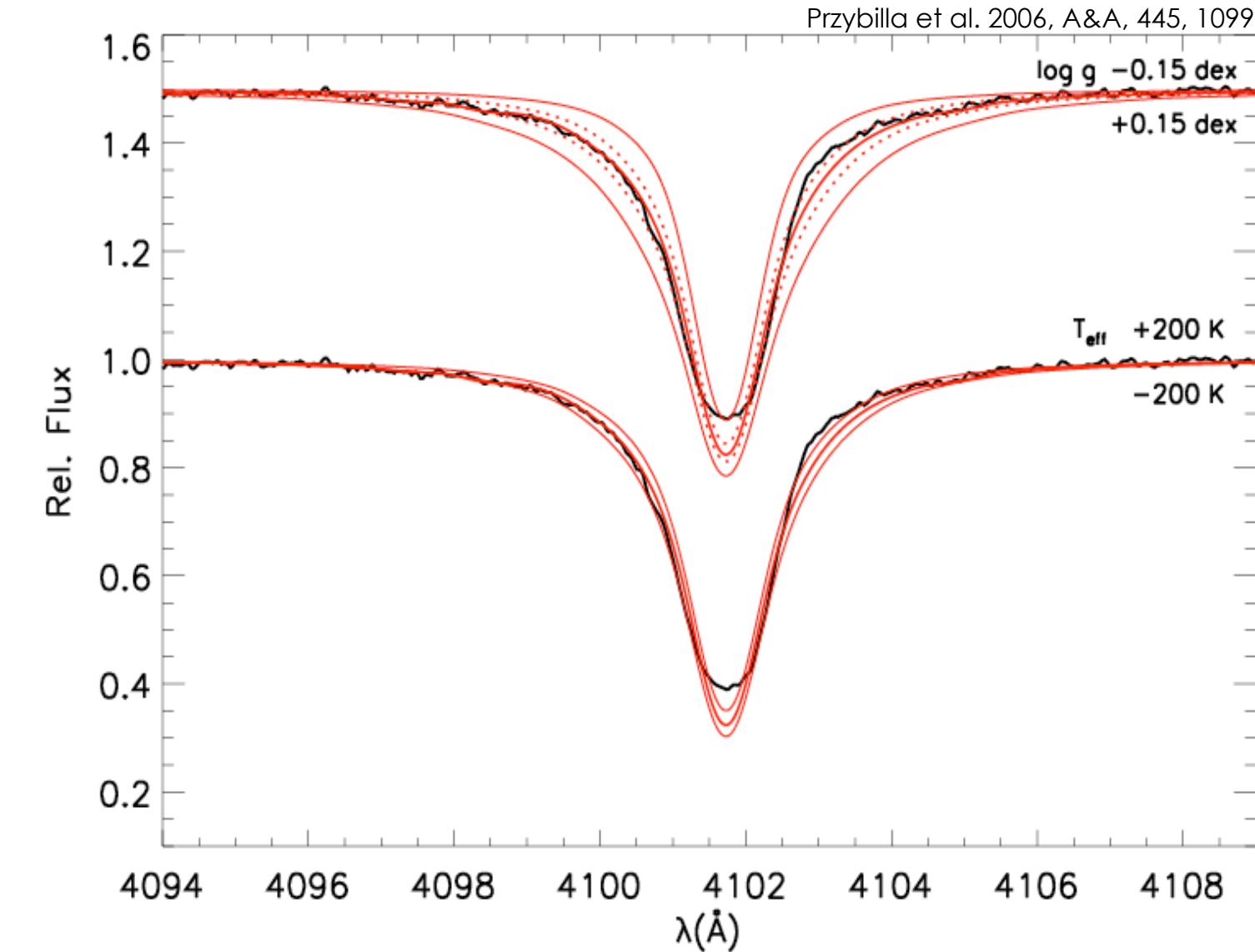
E.g. parameter determination in :

Early-B type dwarf/giant stars
&
A-type supergiants

- $\log g$ & T_{eff} : hydrogen lines (Balmer, Paschen, ...)
- $\log g$ & T_{eff} : ionization equilibria (He, metals)
- ξ : $\varepsilon(X)$ from line analysis vs. observed W_λ
- y : He lines
- [M/H]: abundance analysis
- $v \sin i$ & ζ : line analysis
- additional constraints: SED's, near-IR ...

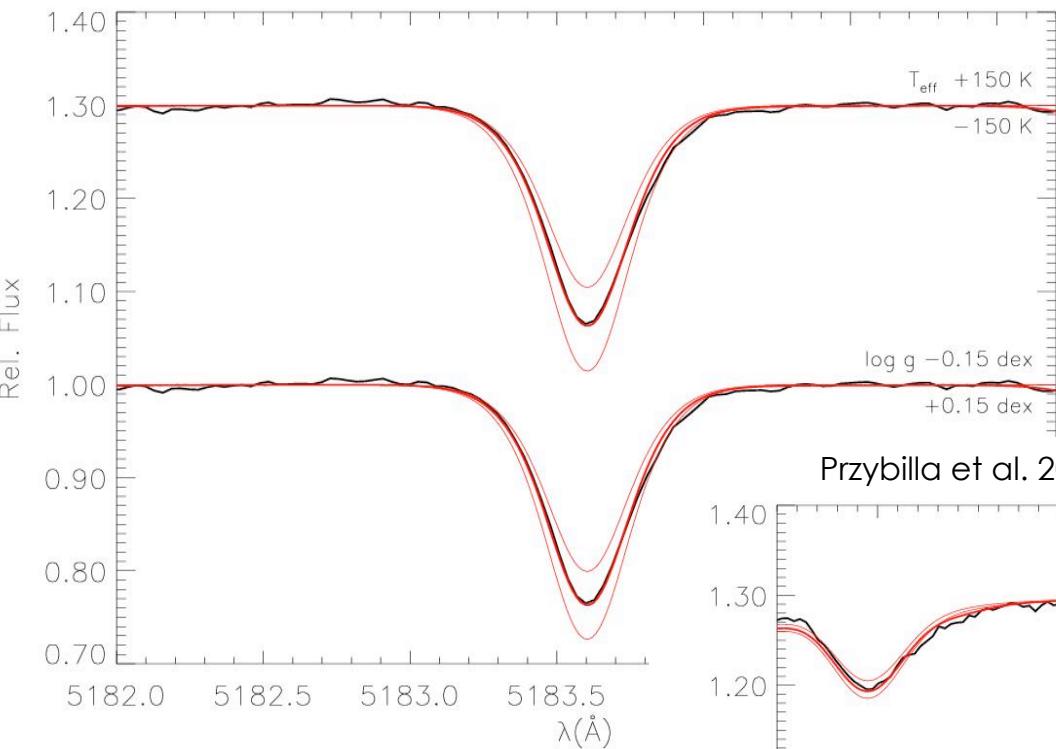


T_{eff} and $\log g$ effects on hydrogen lines



T_{eff} and $\log g$ effects on metal lines

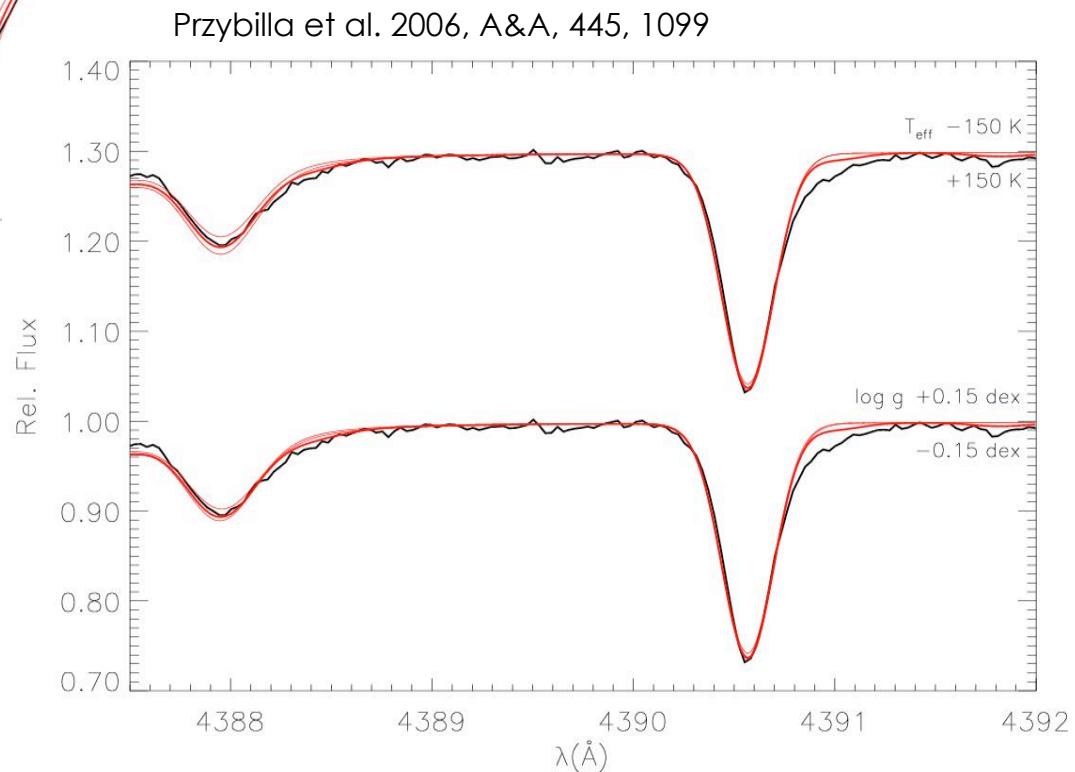
E.g. A supergiant



Mg II non-sensitive

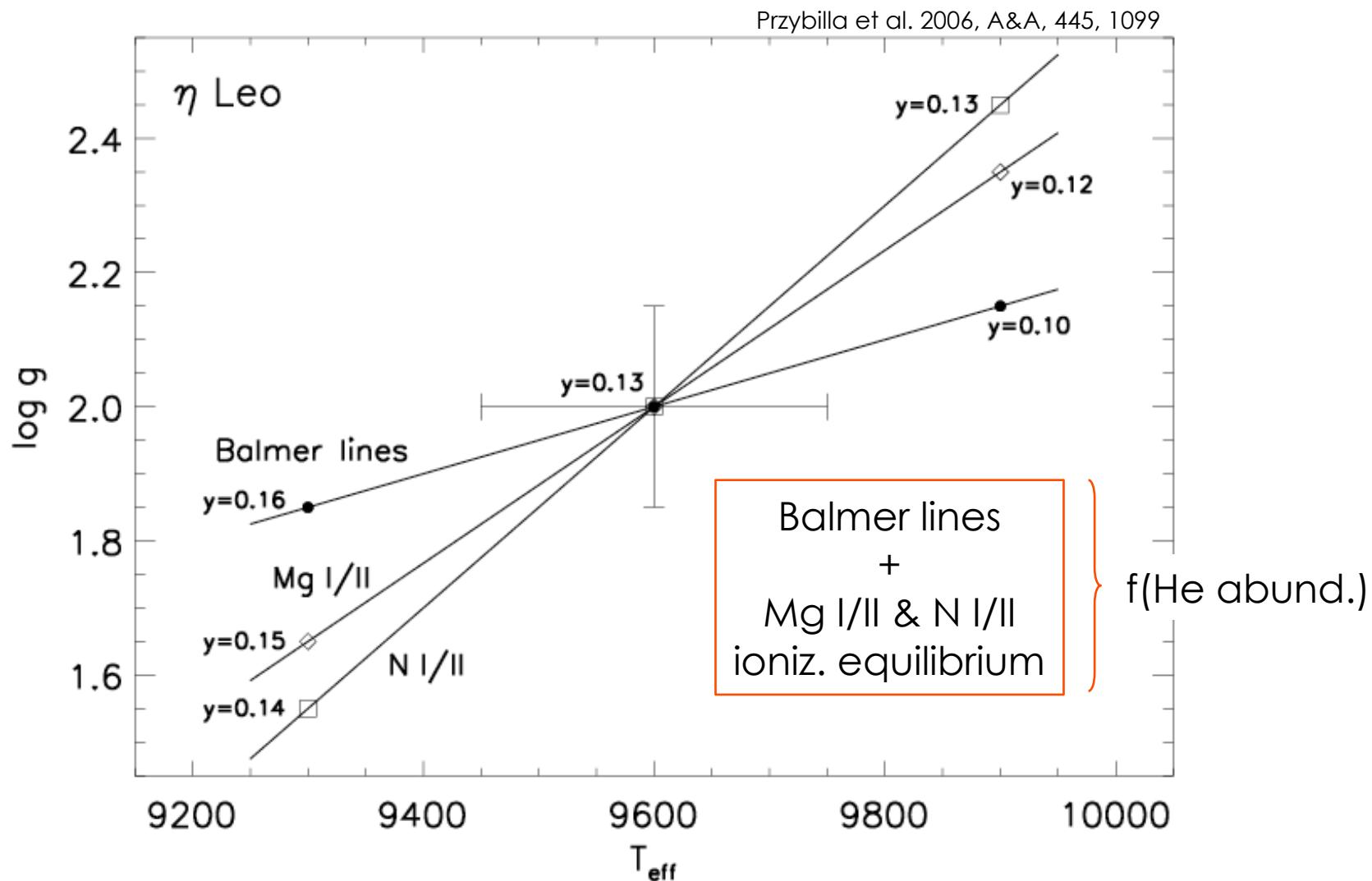
→ ionization equilibrium

Mg I sensitive



T_{eff} & $\log g$ determination from independent indicators

E.g. A supergiant

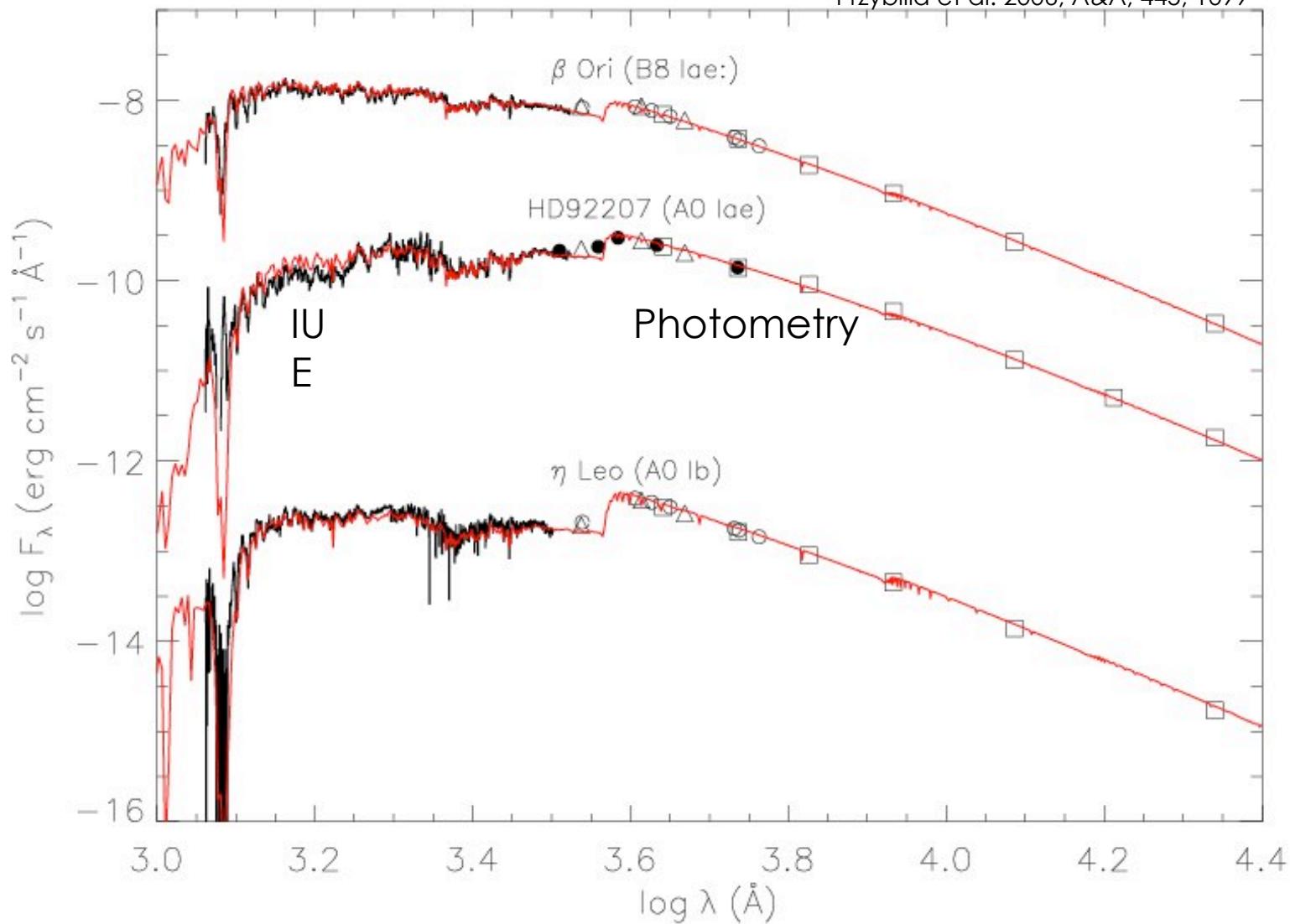


Reduced uncertainties



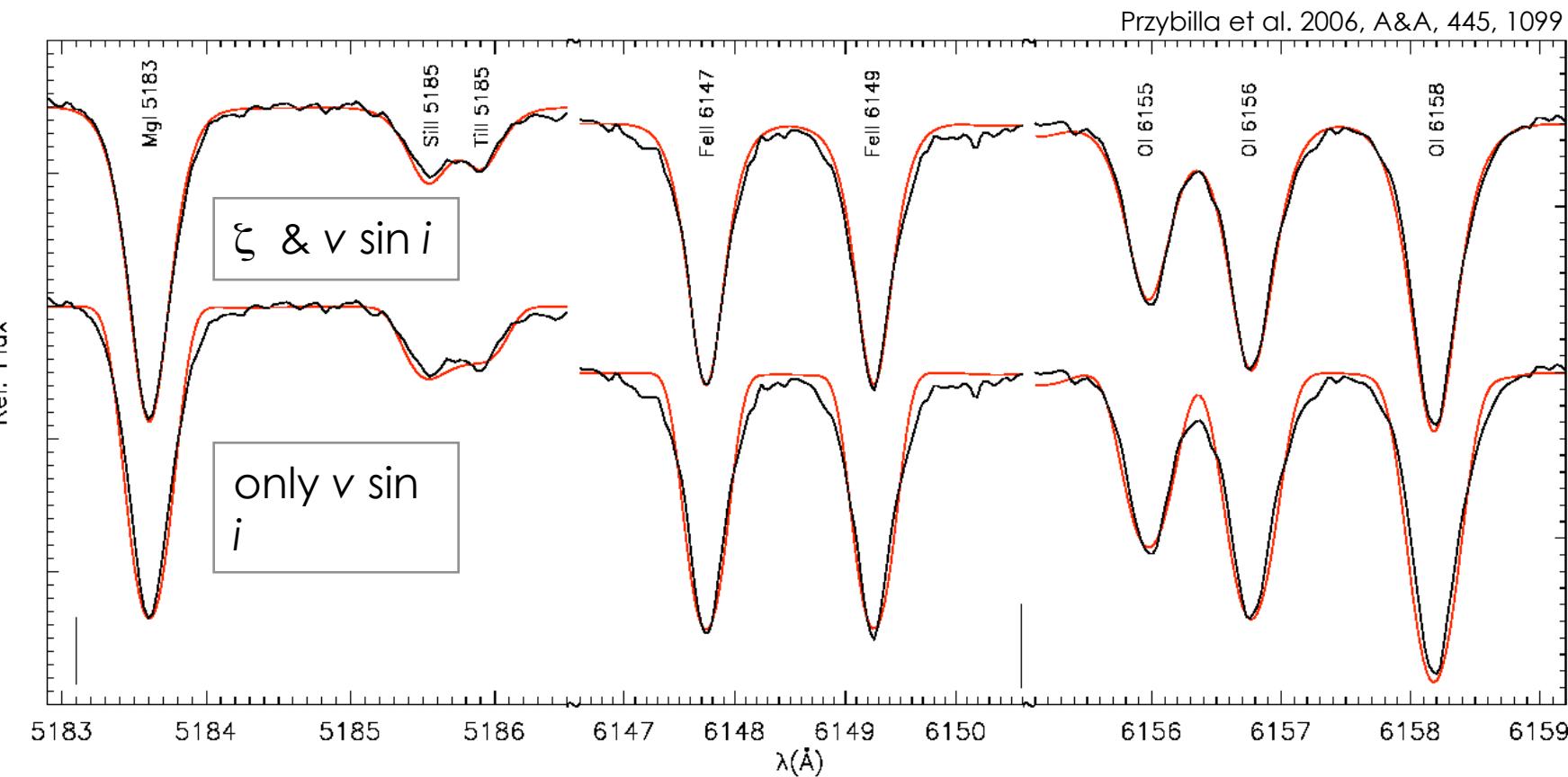
Additional constraint: SEDs

Przybilla et al. 2006, A&A, 445, 1099



Macroturbulence & $v \sin i$ from metal line profiles

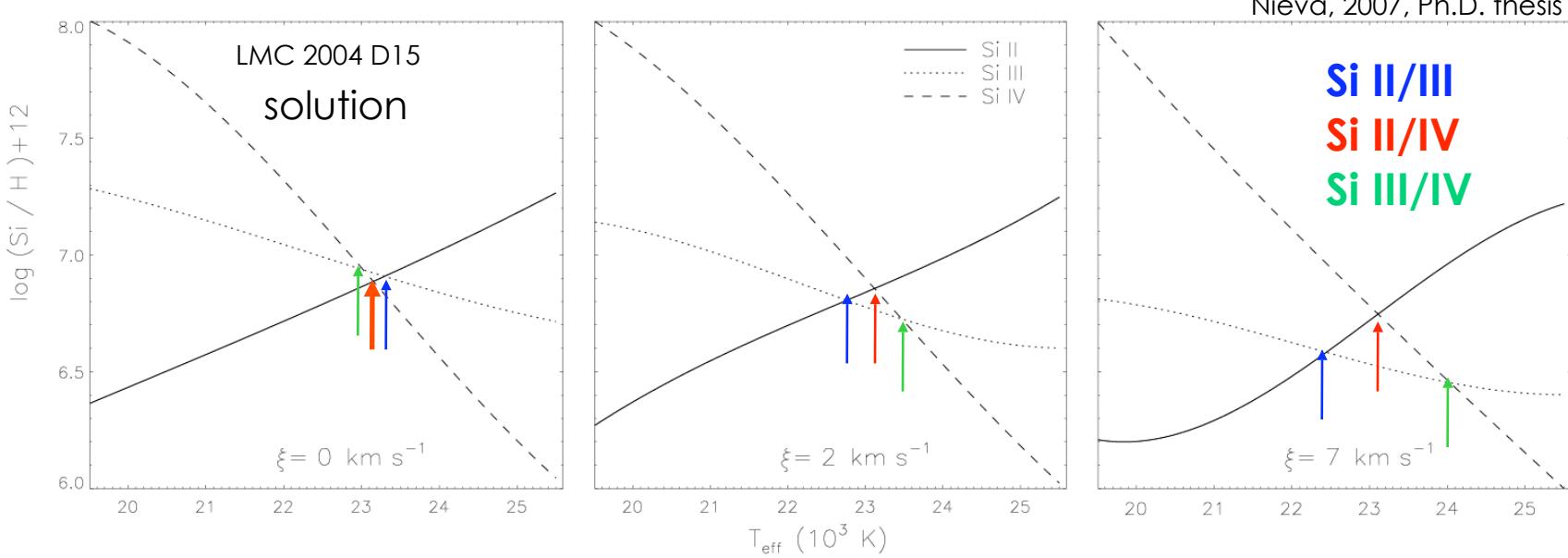
E.g. A supergiant



Advantage of **line profiles** over equivalent widths

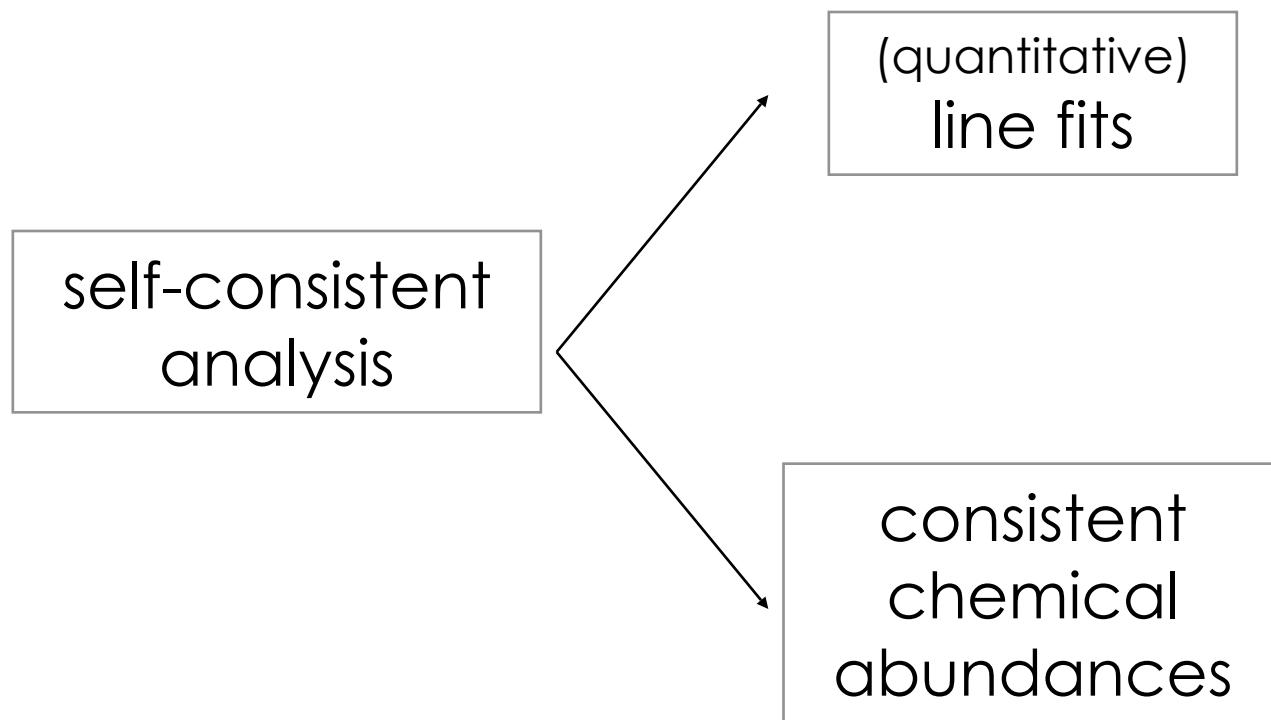
Microturbulence effects on ionization equilibria

E.g. early B dwarf



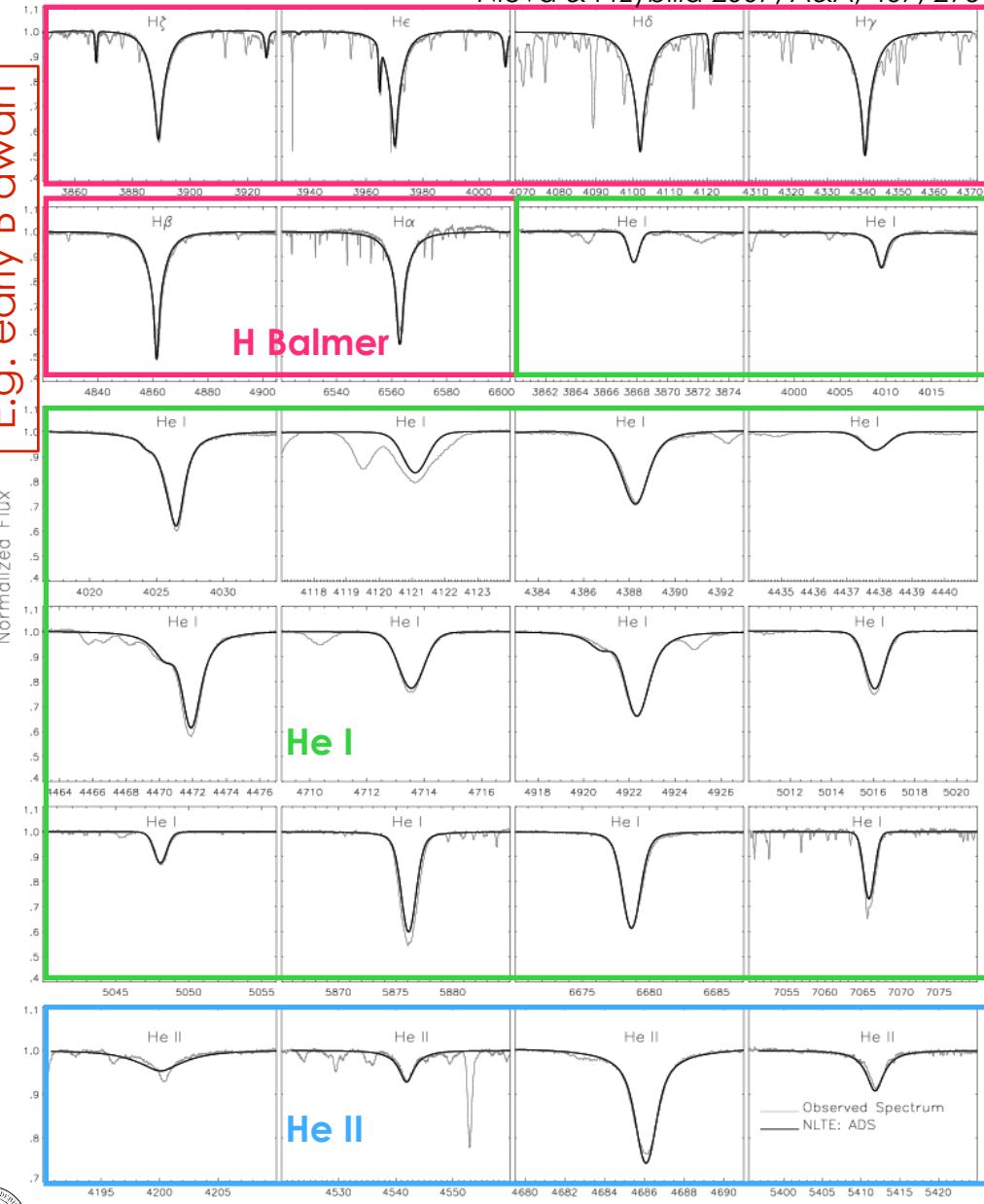
@ $\sim 23000 \text{ K}$ **Si II/IV** lines weak & **Si III** lines strong: sensitive to ξ

Implicit fit to Balmer lines for each T_{eff} (log g determination)

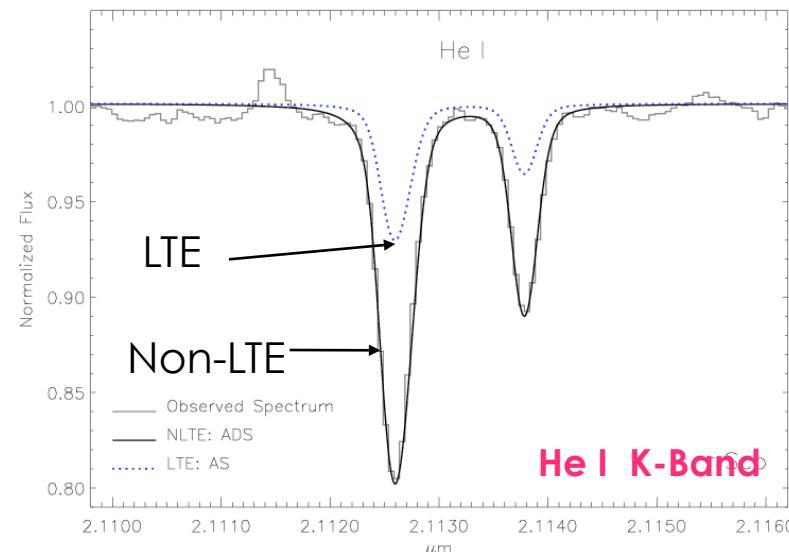
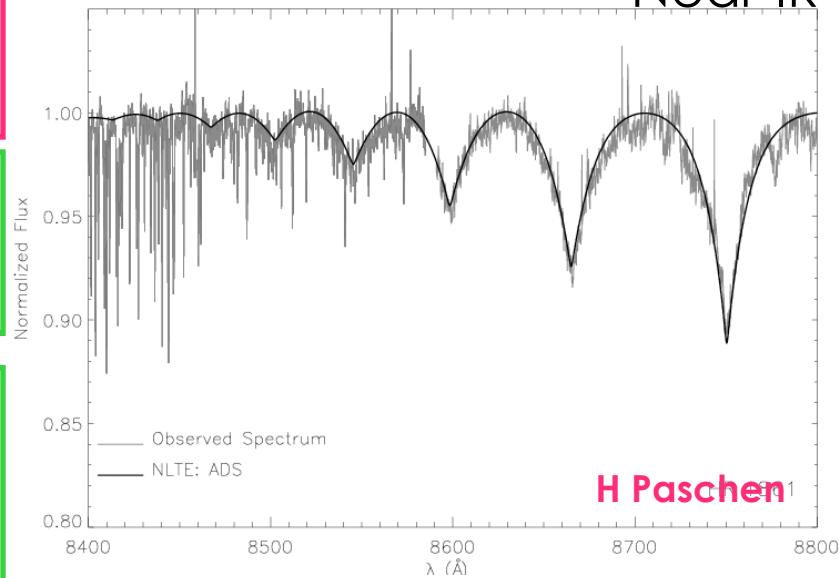


Simultaneous fits to most measurable H/He lines

Visual



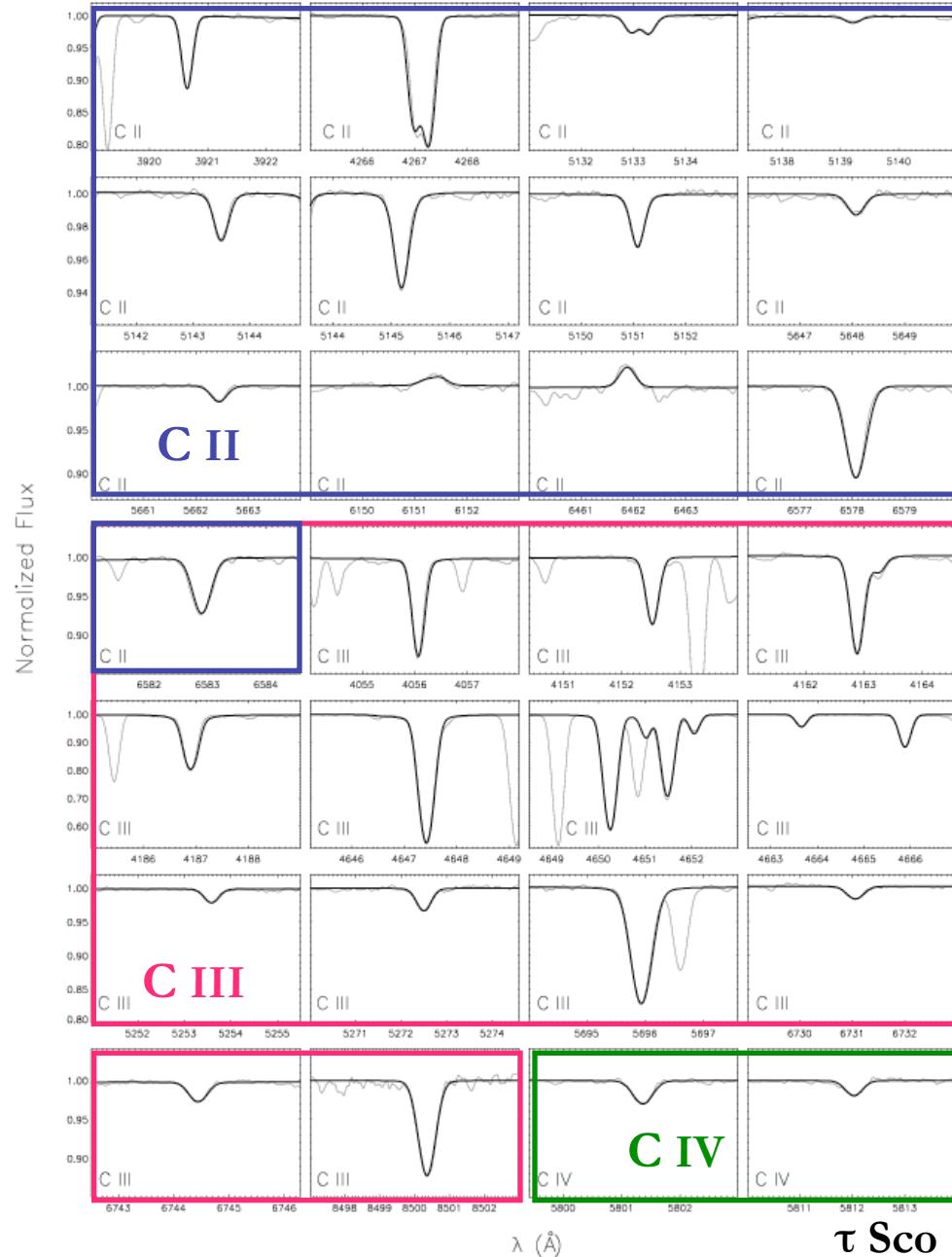
Near-IR



Fits to C lines

E.g. early B dwarf

All lines have very similar abundances
(low 1σ -uncertainties)

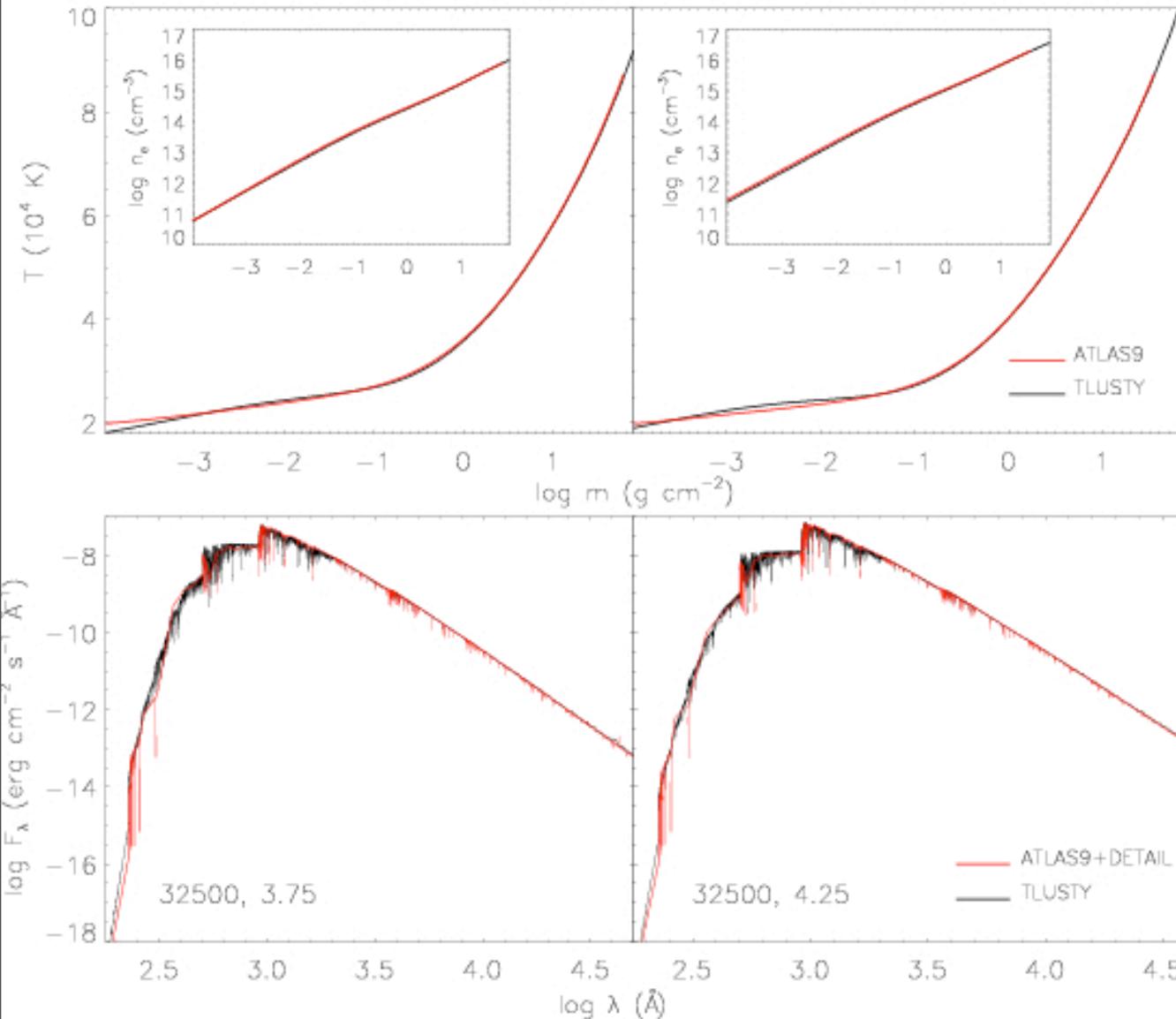


Systematic Uncertainties



E.g. atmospheric structure & stellar flux

Nieva & Przybilla 2007, A&A, 467, 295



metallicity correction:
up to ~ 500 K in line-
formation region

Also:
microturbulence
background
opacities ...

E.g. sensitivity of C II/III/IV abundances to T_{eff} , $\log g$ & ξ variations

E.g. early B giant

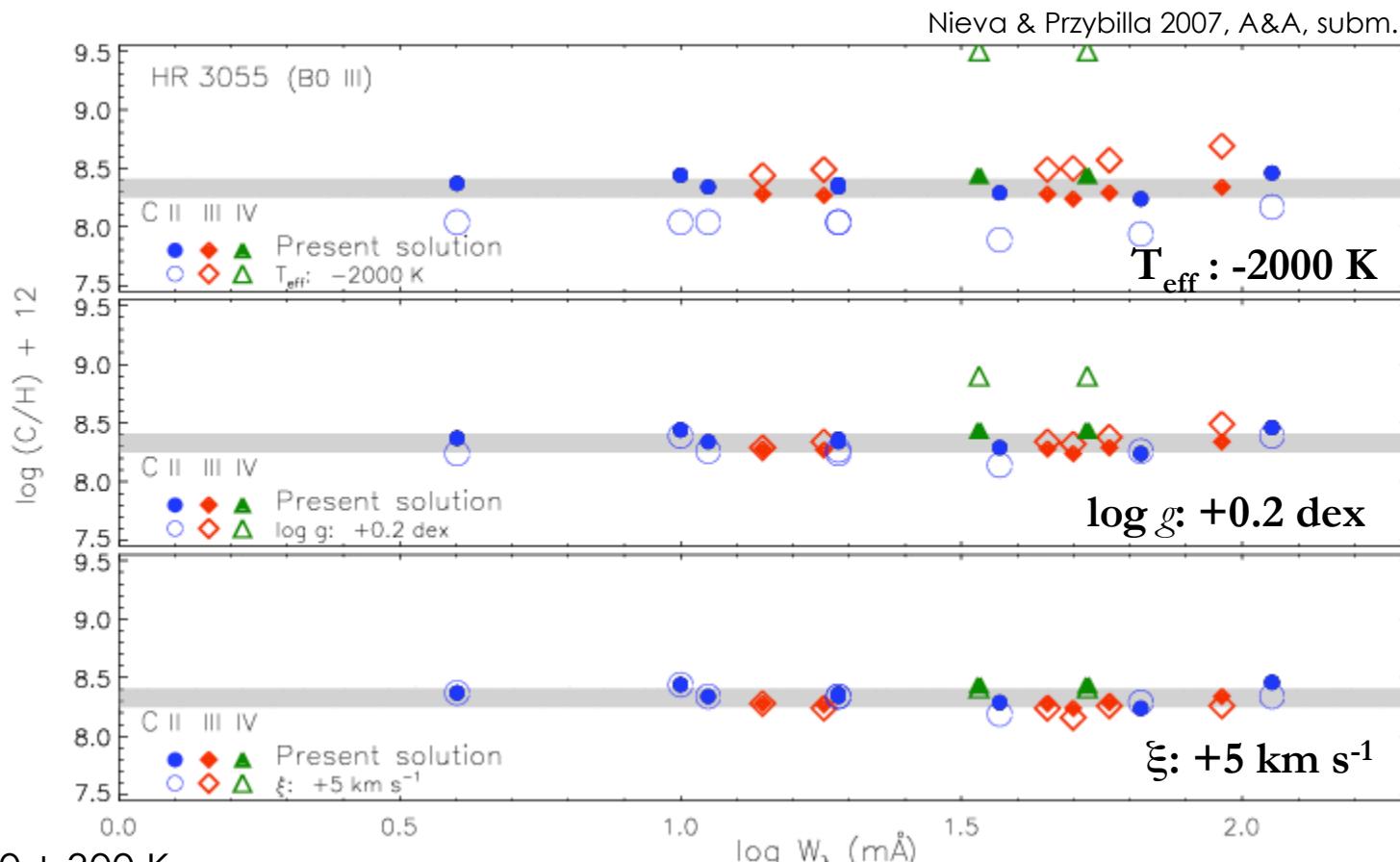
HR 3055

Solution:

$$T_{\text{eff}} = 31200 \pm 300 \text{ K}$$

$$\log g = 3.95 \pm 0.05 \text{ dex}$$

$$\xi = 8 \pm 1 \text{ km s}^{-1}$$



Main effect from T_{eff}

C IV up to **+1.10 dex** ($\sim x10$)
 C III up to **+0.35 dex** ($\sim x2.5$)
 C II up to **-0.40 dex** ($\sim x2.5$)

T_{eff} vs. NLTE effects on C abundances (relative to final results)

E.g. early B giant

		$\Delta T_{\text{eff}} = -2000 \text{ K}$	LTE
HR 3055	C II	4267	-0.33
		5145	-0.32
		5662	-0.33
		6578	-0.40
	C III	4056	+0.21
		4162	+0.28
		4186	+0.35
		4663	+0.22
	C IV	5811	+1.06
			+0.39

Nieva & Przybilla 2007, A&A, subm.

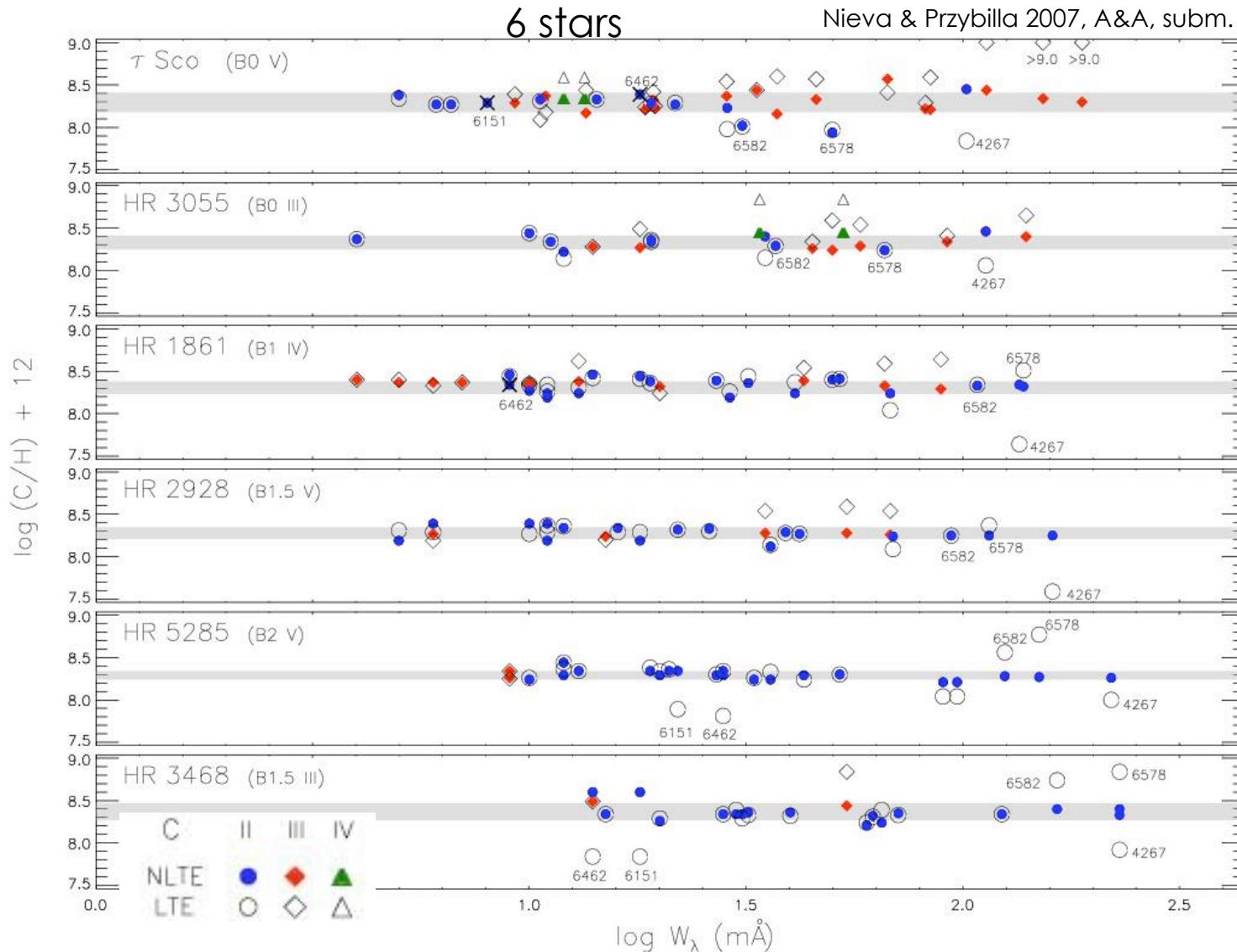


NLTE Results

Consistency is possible after
careful modelling & analysis



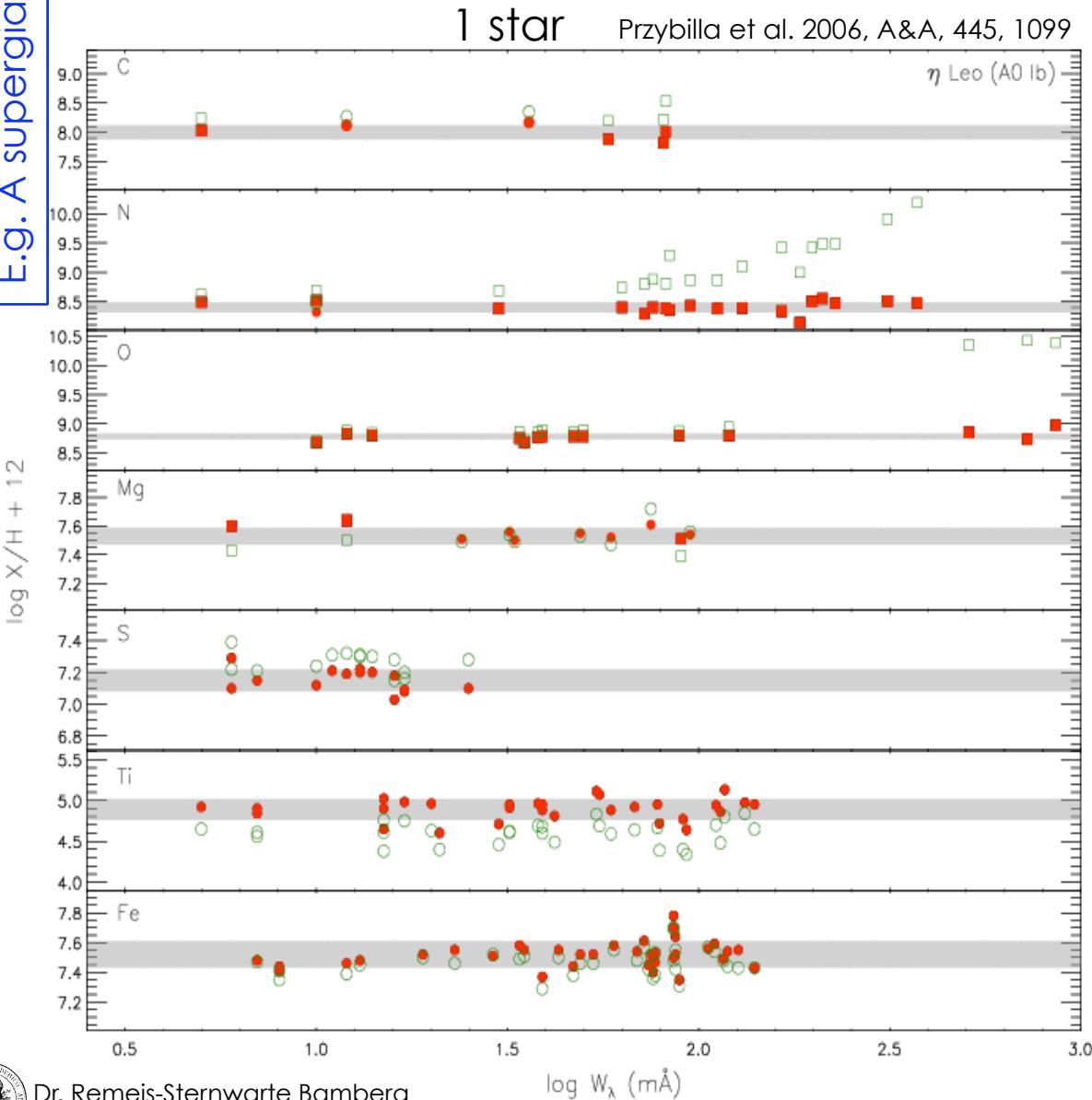
Non-LTE vs. LTE for individual C lines



- NLTE effects different per line & star: constant correction not applicable

Non-LTE vs. LTE chemical abundances

E.g. A supergiant



NLTE:
 absolute abundances
 &
 reduced statistical &
 systematic uncertainties

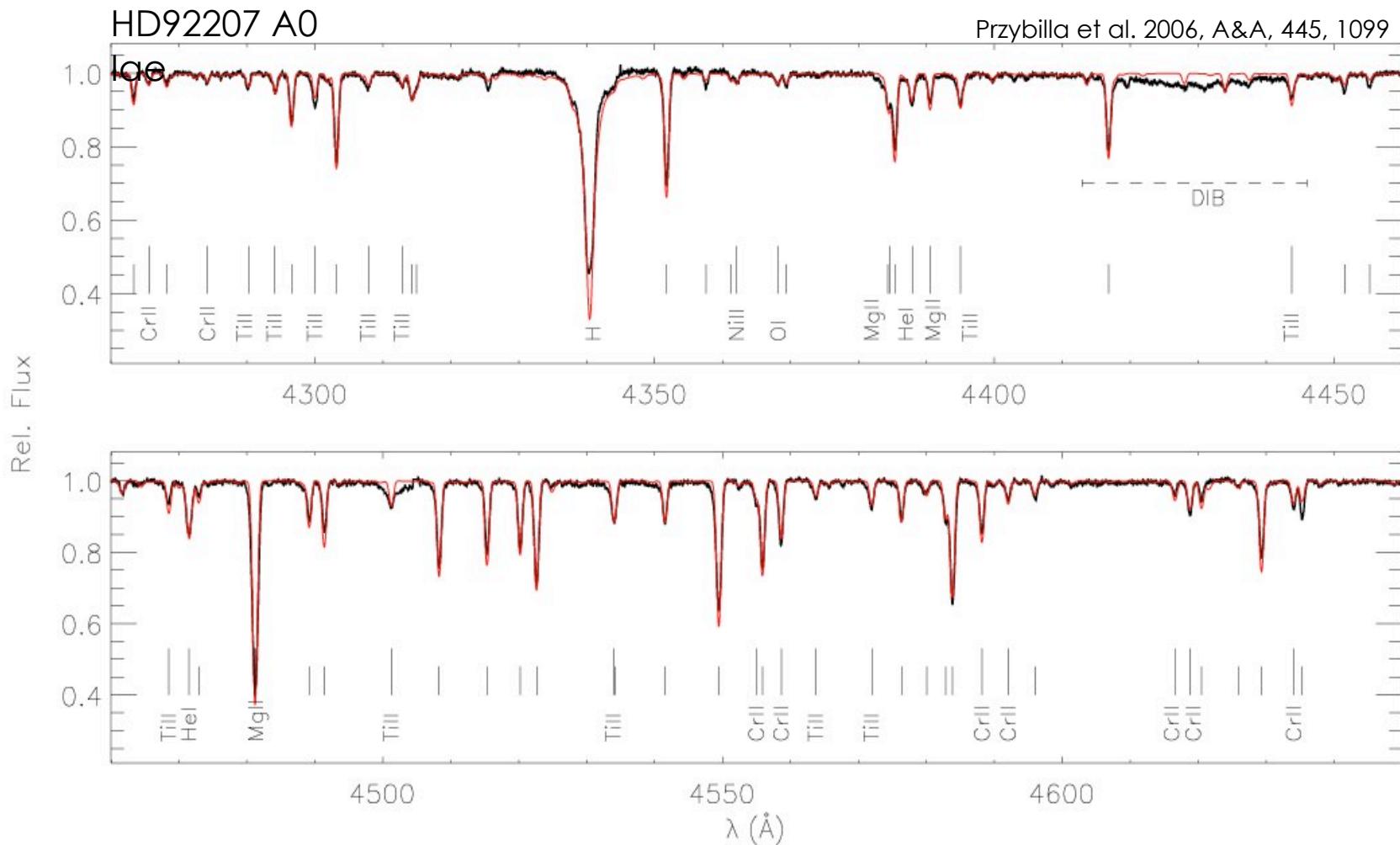
$\Delta \log \epsilon$:
 1 σ -stat.: $\sim 0.05\ldots 0.10$ dex
 1 σ -syst.: $\sim 0.07\ldots 0.12$ dex

typical uncertainties
 in literature (LTE): $x \sim 2\text{-}3$
 + unknown systematic
 errors

NLTE/LTE
■ neutral
○ ionized

Global Spectrum Synthesis

E.g. A supergiant



- good agreement may be obtained in global and in detail