

Non-LTE line formation for trace elements in stellar atmospheres,
July 30 – August 4, 2007, Nice, France

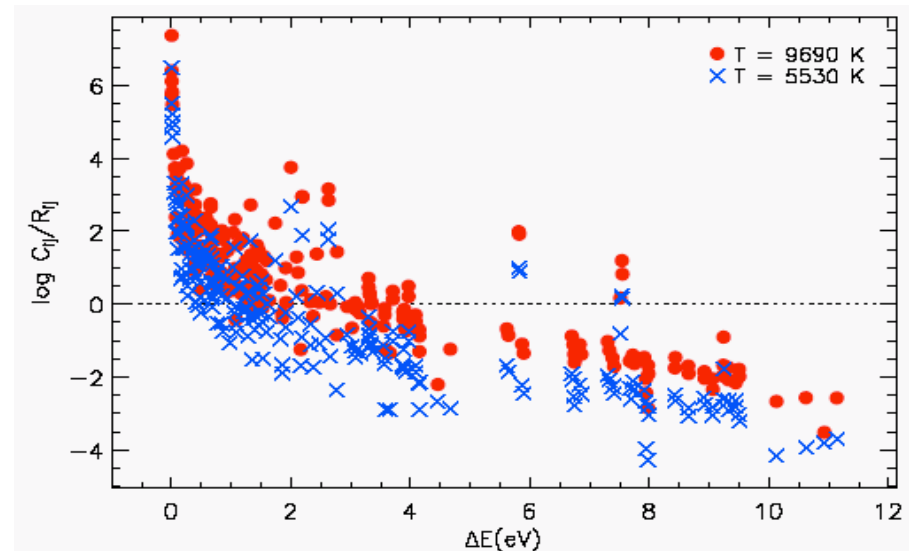
**Accurate collision cross-sections:
important non-LTE input**

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Inelastic collisions versus radiative processes in stellar atmospheres

$\Delta E > 5$ eV, radiative processes
dominate,
 $\Delta E < 0.2$ eV, strong collisional
coupling,
 0.2 eV $< \Delta E < 5$ eV,
accurate collision cross-sections
are particularly important.



C_{ij}/R_{ij} ratios for the Ca II transitions
at $\log \tau_{5000} \cong -0.5$ in the models
5780/4.44 ($T = 5530$ K) and
9400/3.70 ($T = 9690$ K)

Electron impact excitation and ionization

Among all particles the collision frequency is the highest for electrons,

$$v_e / v_A = (m_A / m_e)^{1/2}$$

Sources of cross-sections.

- Laboratory measurements: for the transitions mostly from the ground state of atoms.
- Quantum-mechanical calculations (the R-matrix method in the close-coupling approximation) of collision *excitation* cross-sections exist for the selected atoms and ions.

More data is expected from the Iron Project.

An accuracy is a few 10%.

- Approximation formulae for the majority of the transitions in atoms. Accurate to a factor of 2 to 10.

Collision excitation.

- *Sobelman et al.* (1981) cross-sections in the Born I approximation for neutrals,
- *van Regemorter* (1962) semi-empirical formula for allowed transitions,

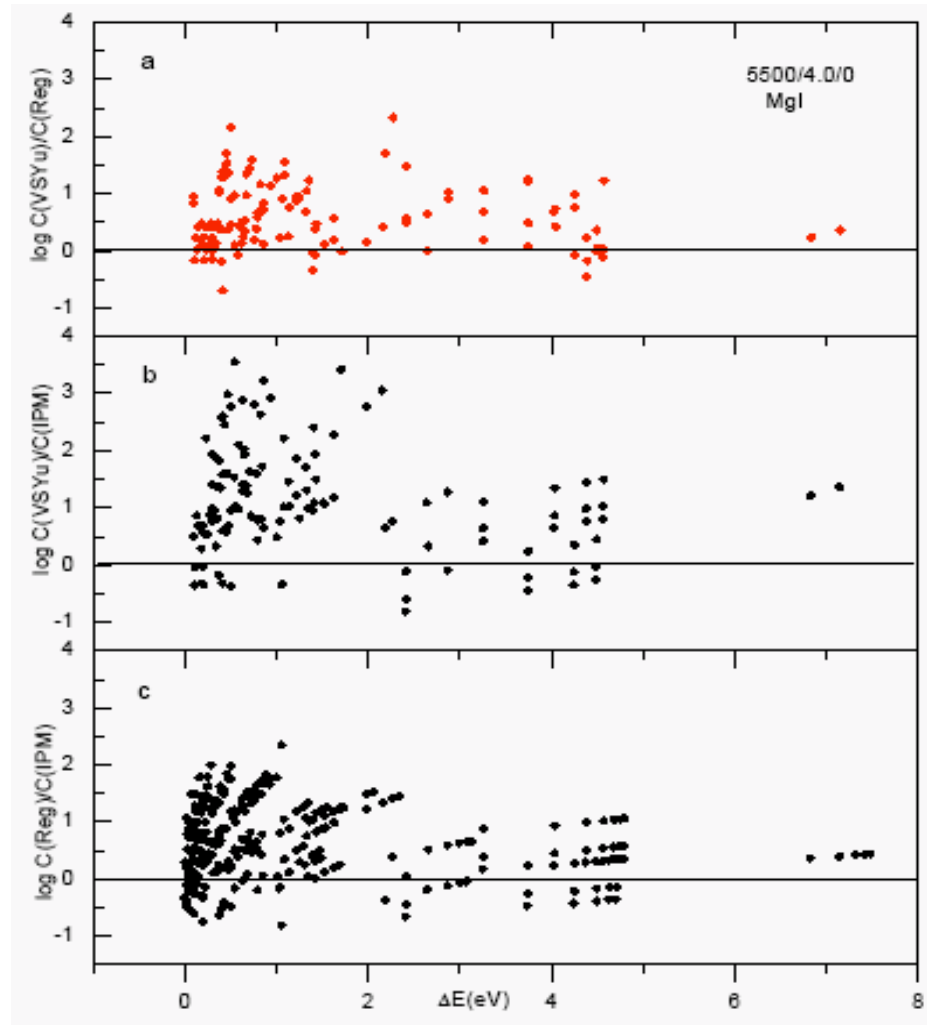
$$C_{ij} = n_e \times 32 \times 10^{-8} f_{ij} \left(\frac{Ryd}{\Delta E} \right)^{3/2} \beta^{1/2} e^{-\beta} P(\beta), \quad \beta = \Delta E / kT$$

- the impact parameter method (IPM, *Seaton* 1962) for allowed transitions,
- the Eissner-Seaton formula for forbidden transitions

$$C_{ij} = n_e \times 8.631 \times 10^{-6} \frac{1}{g_i \sqrt{T}} e^{-\beta} \Omega_{ij} \quad \text{with a collision strength } \Omega_{ij} = 1.$$

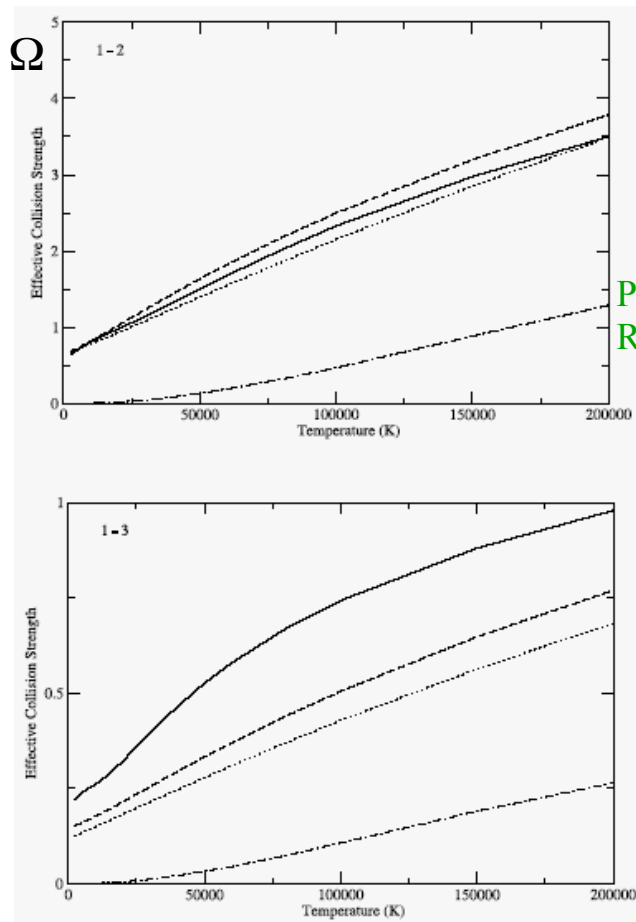
Comparisons among theoretical approximations

- The Born approximation leads to the larger rates compared to those from the van Regemorter formula,
- the van Regemorter rates are larger than the IPM rates



The rate ratios for the transitions in Mg I.

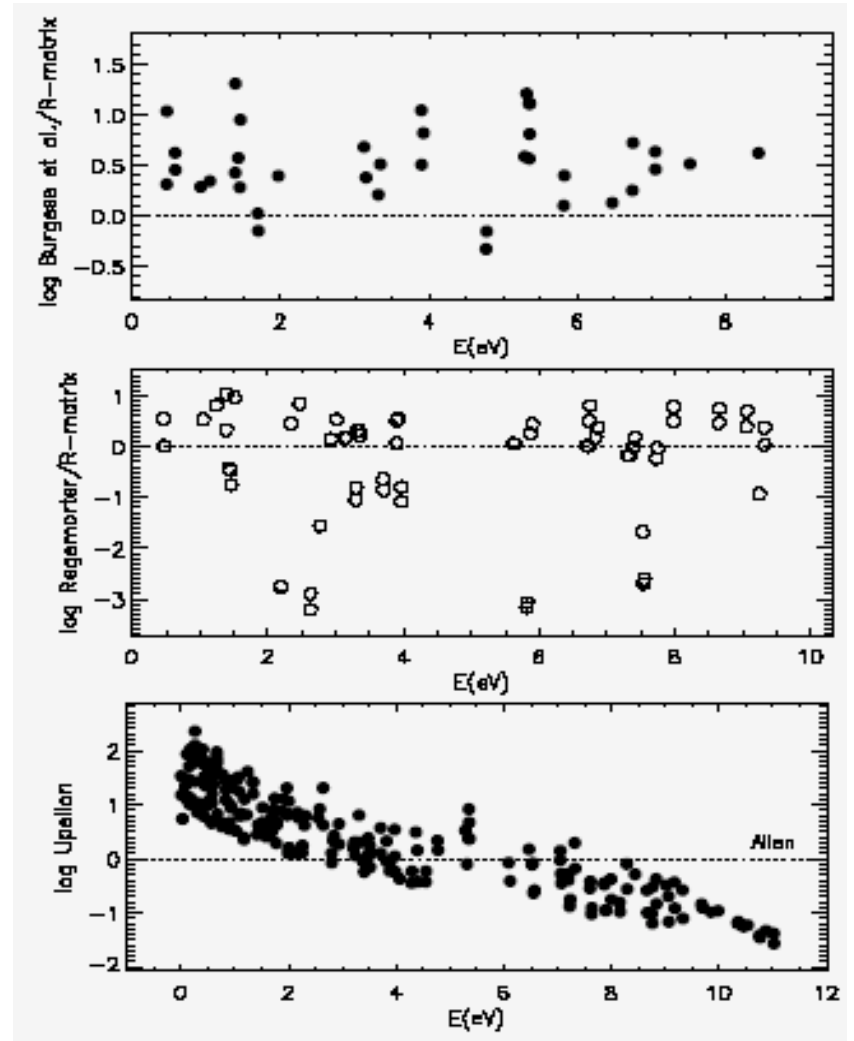
Comparisons of theoretical approximations with the R-matrix method predictions



Persival & Richards 1978

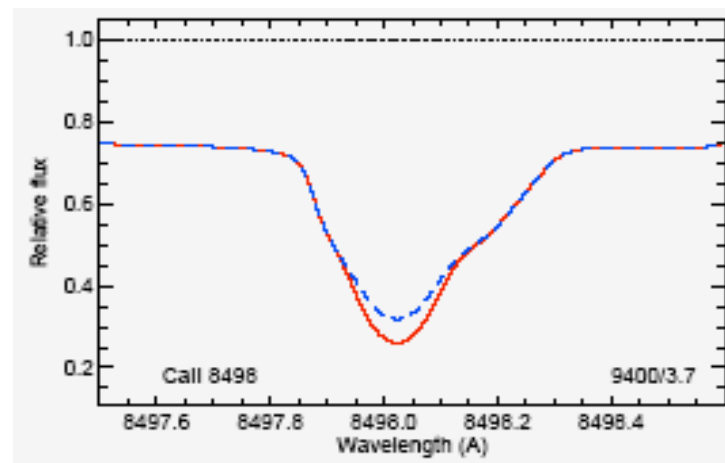
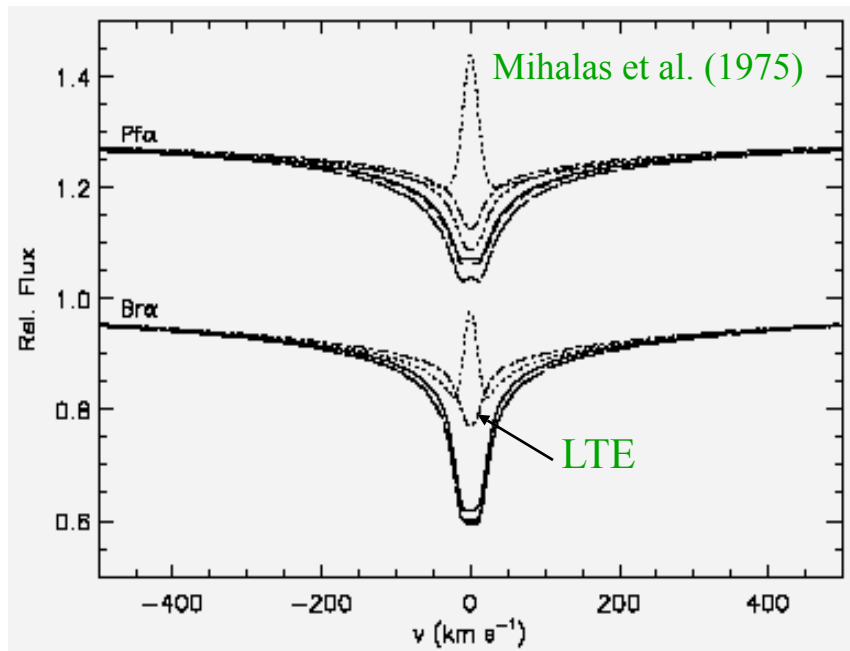
H I, R-matrix method calculations of Butler (continuous line).

Fig. 1 from Przybilla & Butler (2004).



Ca II, R-matrix method calculations of Melendez et al. (2007)

How do the uncertainties in the atomic data translate to uncertainties in the non-LTE modelling?



Non-LTE profiles for Ca II 8498 in the model 9400/3.7 for the R-matrix method data (continuous line) and approximation formulae (dashed line).

Theoretical profiles for Pf α and Br α in Vega for various electron collision rates.

(Przybilla & Butler 2004)

Effect on abundance determinations

The van Regemorter rates vs. the IPM rates
for $T_{eff} = 6000$ K, $\log g = 4.0$, $[Fe/H] = 0$ to -3 .

A change in $\Delta_{NLTE} = \log \epsilon(NLTE) - \log \epsilon(LTE)$:

≤ 0.03 dex for different lines of Ca I,

0.07 dex to 0.14 dex for different lines of Ca II.

(Mashonkina et al. 2007a)

Collision ionization

For the excited levels:

semi-empirical formulae based on the classical Thomson theory.

They should provide data accurate to a factor of 2 or better.

The *Seaton* (1962) formula:

$$C_{ik} = n_e \times 1.55 \times 10^{13} \alpha_{i,thr} \frac{\bar{g}_i}{\beta \sqrt{T}} e^{-\beta}$$

Here, $\alpha_{i,thr}$ is the threshold photoionization cross-section,

$$\bar{g}_i = 0.1, 0.2, \text{ and } 0.3 \text{ for } Z = 1, 2, \text{ and } \geq 3.$$

Inelastic collisions with hydrogen atoms

In the atmosphere of solar-type stars, $n_H/n_e \geq 10^4$.

Cross-sections ?

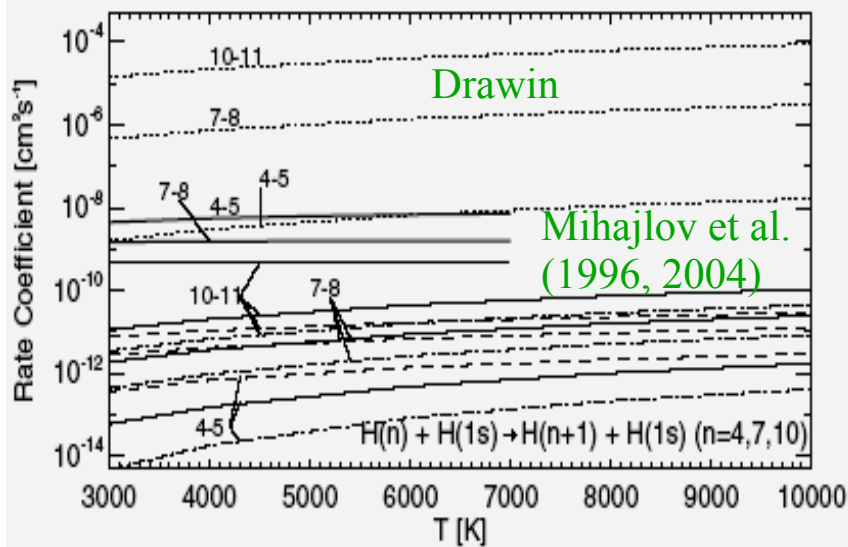
- Low-energy experimental data
(for only the very lowest states of Na I, *Fleck et al.* 1991),
- quantum mechanical calculations
(for the transitions between low-excitation levels in Li I, *Belyaev&Barklem* (2003) and Na I, *Belyaev et al.* (1999)),
- some theoretical approximations for the system $H(n) + H(1s)$
(see review and detailed discussion in *Barklem*, 2007),
- the approximation formula of *Drawin* (1968,1969). This is a semi-empirical modification of the classical Thomson formula for ionization by electrons.

Data comparisons

- The Drawin's formula vs. experimental data and quantum mechanical calculations.

The resonance transitions in Li I and Na I: the classical formula overestimates the cross-sections by **3 dex to 5 dex**.

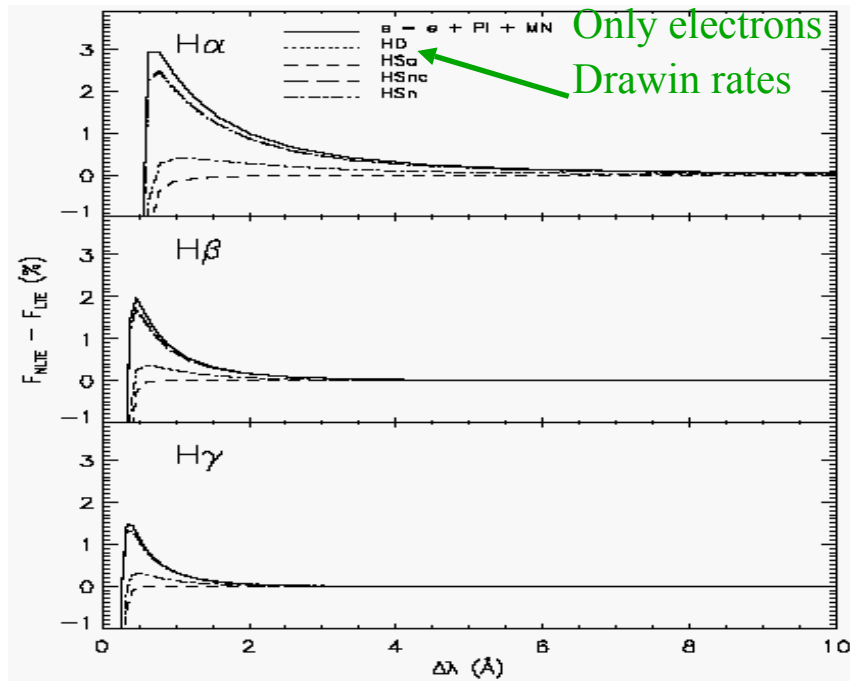
Barklem (2007)



Excitation rates for the $n - (n+1)$ transitions in H I from different approximations

- The Drawin's formula vs. the semi-classical data of *Mihajlov et al.* (1996, 2004) for H I. For the transition 4 – 5, a consistency within **a factor of 2**. A discrepancy increases up to **3 dex / 5 dex** for $n = 7 / n = 10$.

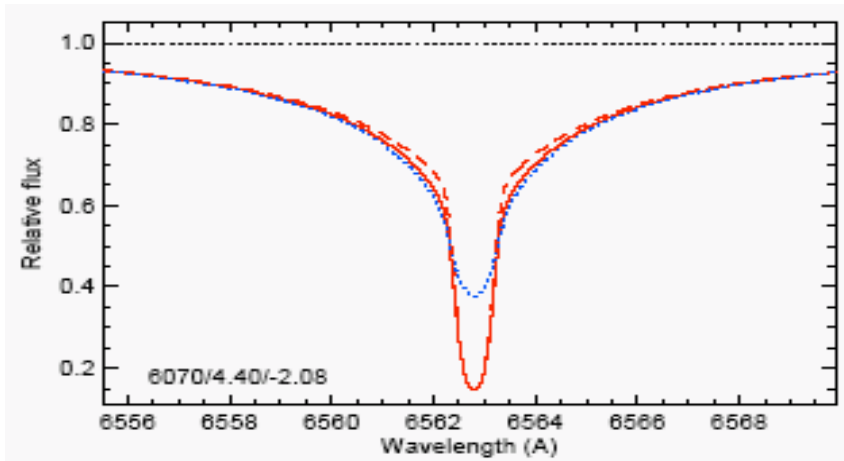
How do the uncertainties in the atomic data translate to the uncertainties in non-LTE modelling?



Hydrogen collisions à la Drawin are relatively unimportant for the SE of H in the Sun.

Barklem (2007): the differences between the non-LTE and LTE profiles for different collisional data, MACKKL solar model.

How do the uncertainties in the atomic data translate to the uncertainties in non-LTE modelling?



The effect of the inclusion of the Drawin hydrogen collisions (continuous curve) for the metal-poor model.

Dashed curve: only electronic collisions.

Dotted curve: LTE.

(Mashonkina et al. 2007b):

6070/ 4.4/-2.08:

The inclusion of the Drawin hydrogen collisions leads to a 100 K lower T_{eff} from H_{α} .

Experimental and quantum mechanical data predict a minor role of hydrogenic collisions in the SE of atoms.

What do observations say?

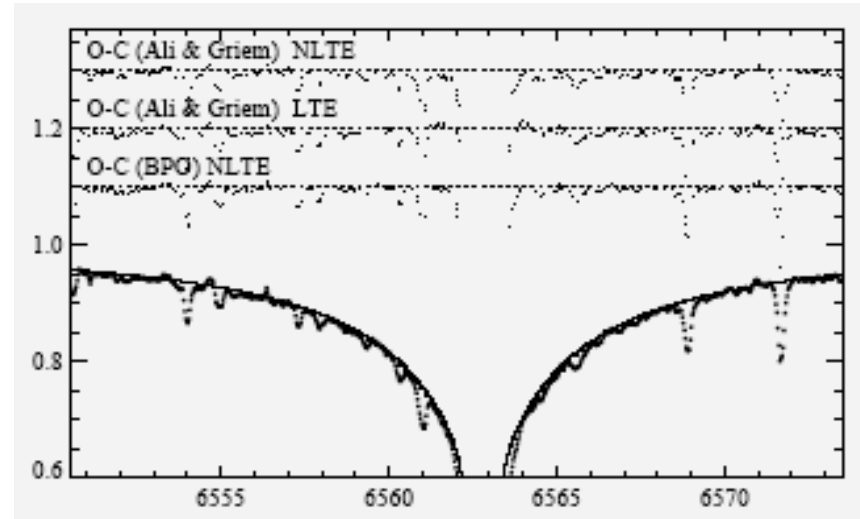
Empirical estimation of the efficiency of hydrogen collisions

It is represented by a scaling factor S_H applied to the Drawin's formula as described by Steenbock&Holweger (1984).

- H I: S_H can be estimated from achieving a consistency of T_{eff} derived from H_α and H_β .

Mashonkina et al. (2007b):
for four VMP ($[Fe/H] < -2$) stars,
 $S_H = 1$ to 2.

Example: BD+3°740
($\log g = 3.90$, $[Fe/H] = -2.65$).
 $T_{eff} = 6340$ K from H_β .
 $T_{eff} = 6440$ K from H_α , $S_H = 0$.



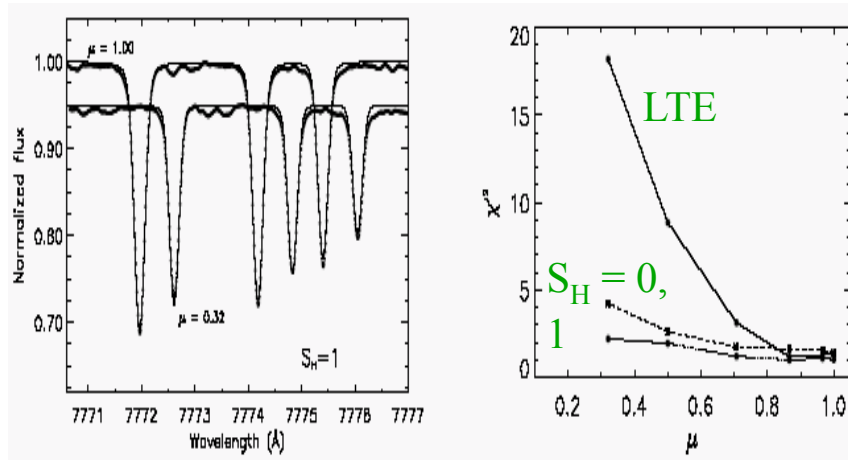
H α in BD+3°740 (bold dots).

LTE: $T_{eff} = 6280$ K,

non-LTE ($S_H = 2$): $T_{eff} = 6340$ K.

Empirical estimation of S_H

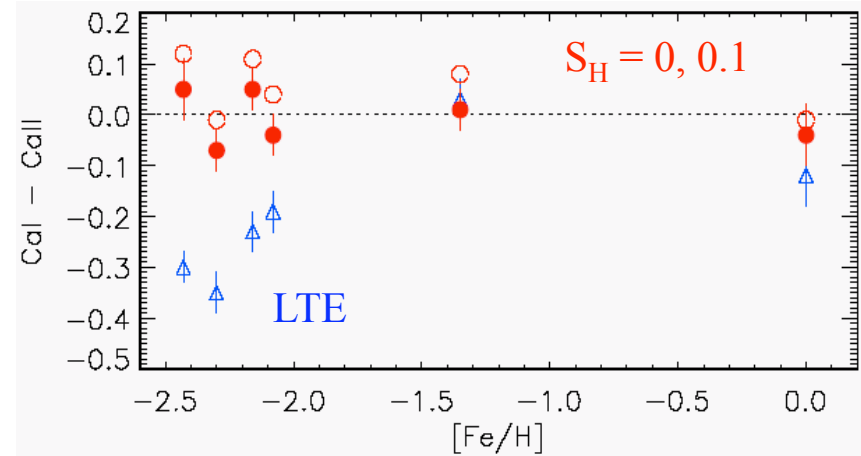
- from studying the center-to-limb variation of solar Na I 6160 and O I triplet $\sim 7770 \text{ \AA}$
(Allende Prieto et al. 2004)



$S_H = 1$ from
O I $\sim 7770 \text{ \AA}$,
 $S_H = 0$ from
Na I 6160

Variation in
the quality
of the fits

- from the CaI/CaII ionization equilibrium in the Sun and selected metal-poor stars
(Mashonkina et al. 2007a)

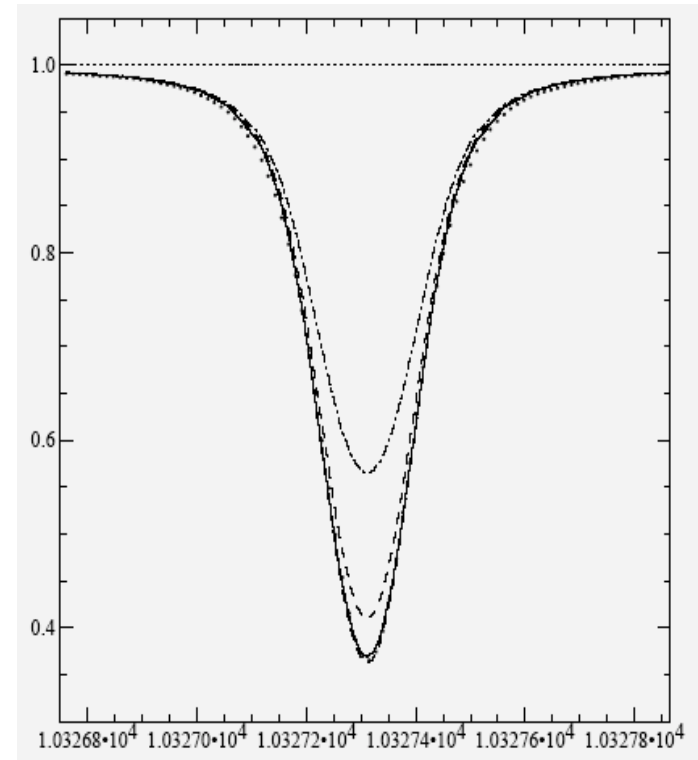


$S_H = 0.1$

Empirical estimation of S_H

Mashonkina&Gehren (2001)

- Solar line profile fitting.
 - O I: $S_H = 1$ (*Takeda 1995*),
 - Na I: $S_H = 0.05$ (*Gehren et al. 2004*),
0.1 (*Takeda 1995*),
 - Al I: $S_H = 0.002$ (*Gehren et al. 2004*),
 - K I: $S_H = 0.05$ (*Zhang et al. 2006*),
 - Sr II, Ba II: $S_H \cong 0$
(*Mashonkina&Gehren 2000, 2001*)
- Spectral analysis of RR Lyr type stars (*Gratton et al. 1999*).
 - O I: $S_H = 3$,
 - Na I: $S_H = 0.01$,
 - Mg I: $S_H = 3$,



Sr II 10327 in the Sun (bold dots)
 $S_H = 0$ (long-dashed curve),
0.01 (continuous curve),
0.1 (dashed curve), and
LTE (dash-dotted curve).

Concluding remarks

- Collisional data used in non-LTE calculations have various degrees of accuracy.
- A practice points to the existence in stellar atmospheres of some thermalization processes in addition to electronic collisions.
- The empirical estimates of the efficiency of hydrogen collisions are obtained to be rather different for different atoms.
- The collisional efficiency may well differ from element to element and transition to transition.
- A calibration may mean that any modelling deficiency (atmospheric structure, atomic data, stellar parameters, etc.) is simply hidden in S_H .